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ARTICLE

Hydrocarbon Generation Potential Evaluation of Coal Shale Gas of Permo-Carboniferous in Jiyang Depression

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Shale gas
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ABSTRACT

In order to study the hydrocarbon-generating potential of Carboniferous-Permian coal shale in Jiyang Depression, geochemistry, petroleum geology and coal geology were applied to study the residual strata distribution of Carboniferous-Permian in Jiyang Depression, organic matter abundance, organic matter types and organic matter maturity of mudstone. The results show that the thickness of the Carboniferous-Permian residual strata in Jiyang Depression is generally 200-800 m, with a maximum thickness of 900 m; the organic matter abundance of coal-bearing shale is good, and it is type III kerogen, which is conducive to gas generation, and the maturity of organic matter reaches a mature-higher maturity stage; the hydrocarbon generation potential of Benxi Formation and Taiyuan Formation is better; Medium to good hydrocarbon source rocks is able to be found in every sag of Shanxi Formation hydrocarbon source rocks, but the scope is limited, and the overall evaluation is still medium. Generally speaking, the Permo-Carboniferous coal-bearing shale in Jiyang Depression has certain shale gas exploration potential.

1. Introduction

Shale gas refers to natural gas in dark mud shale, which is mainly adsorbed and free. Essentially, it is a continuous generation of biochemical gas, thermogenic gas or a mixture of both [1–3]. The formation and distribution of shale gas have unique characteristics. Shale gas often distributed in the effective source rocks with large thickness and wide distribution in the basin, which has the advantage of large resource potential and long exploitation life [4–8]. Conventional wisdom holds that source rock can only produce oil and gas but cannot store oil and gas. However, with the development of times, it is gradually found that source rocks can not only generate natural gas but also store a large amount of natural gas [7–8]. Therefore, it is not too much to say that the formation of shale gas reservoirs is due to the adsorption of shale formation and hydrocarbon residue caused by low formation permeability [9]. However, cracks and voids in mud shale become the space where oil and gas occur, so a large part of the gas is retained in the mud shale stratum (“shale gas”) [10].

The Jiyang Depression is located in the south of the Bohai Bay Basin. Where the Carboniferous-Permian is relatively developed. A large number of dark shales are
developed in Benxi Formation, Taiyuan Formation and Shanxi Formation, which are important source rocks because of their rich organic matter \[10-13\]. The Carboniferous-Permian sandstone reservoir in this area is object of exploration. Coal-derived gas from the Carboniferous-Permian coal-bearing source rocks was found in the Shihezi Formation sandstones \[14\], but the research on coal-bearing shale gas was relatively less. In this paper, the hydrocarbon generation potential of shale in Carboniferous-Permian in Jiyang Depression is studied by geochemical method, and the shale gas resource potential is determined, which has certain guiding significance for shale gas exploration in this area.

The abundance of organic matter is used to represent the relative content of organic matter in rocks, and to measure and evaluate the hydrocarbon generation potential of rocks. At present, there are three indicators to measure: the total organic carbon content (TOC), rock pyrolysis hydrocarbon generation potential (S1+S2) and hydrocarbon index (HI) \[7,8,10-13\]. The hydrocarbon generation potential of shale in the Benxi, Taiyuan and Shanxi Formations has studied in detail. Among them, the Benxi Formation and the Taiyuan Formation are products of the epicontinental sea environment, while the Shanxi Formation is the formation of the deltaic environment \[25\]. Therefore, combining with sedimentary environment, the hydrocarbon generation potential of Benxi Formation and Taiyuan Formation and Shanxi Formation is discussed in this paper.

2. Regional Geological Survey

Jiyang Depression is a first-order negative tectonic unit, which converges westward and spreads eastward near east-west direction and is hosted by Chengning uplift and Luxi uplift in Bohai Bay Basin \[13,18\]. It is bounded by Chengning uplift in the north, Luxi uplift in the south, Bohai Sea in the East and Linqing block fault basin in the west \[11-13\]. The depression includes Chezhen, Zhanhua, Huimin and Dongying sags \[16\] (Figure 1). The Carboniferous-Permian system in Jiyang Depression is similar to the whole North China area. In the late Ordovician of Early Paleozoic, due to the influence of Caledonian movement, the whole uplift was denuded, and the deposits of Upper Ordovician, Silurian, Devonian and Lower Carboniferous were missing. From the Late Carboniferous, the North China Platform was re-subsided and deposited, and a set of coal-bearing strata of marine-continental interaction was formed in the Late Permian. There are two sets of obvious sedimentary assemblages: from late Carboniferous to Early Permian, Jiyang Depression is a large epicontinental sea basin like North China. It deposited a set of “sea-land alternating” coal-bearing strata, that is, the main hydrocarbon-rich strata of Carboniferous-Permian. From early Permian to the end of Late Permian, Jiyang Depression is a large continental depression basin and has deposited a set of continental strata, which basically did not contain marine deposits and had poor coal-bearing property \[17\]. Thickness of the residual Carboniferous-Permian is generally 400-1000 m, and the maximum thickness is estimated to be about 1200 m. The thickness of dark mudstone and carbonaceous mudstone is 50-250 m. The maximum thickness of coal seam is 44.5m \[18\]. The coal-bearing strata in this area are Benxi Formation, Taiyuan Formation, Shanxi Formation, Lower Shihezi Formation and Upper Shihezi Formation \[19-21\]. Among them, Benxi Formation, Taiyuan Formation and Shanxi Formation are coal-bearing strata. The sedimentary environment of the Benxi Formation and the Taiyuan Formation is epicontinental marine environment, while the Shanxi Formation is formed in the river-controlled shallow water delta sedimentary environment \[22\].

![Figure1. Geographical location map of the study area and tectonic unit of Jiyang Depression](image)

3. Coal-bearing stratum distribution

Jiyang Depression is relatively complete. From Archean to Cenozoic, except for the lack of Upper Ordovician, Silurian, Devonian and Lower Carboniferous, the rest of the strata are distributed in \[23\]. Carboniferous-Permian source rocks are abundant, mainly coal and dark mudstone \[24\]. Drilling data have confirmed that the Carboniferous-Permian strata are distributed in every depression of Jiyang Depression \[25\]. Drilling into the Carboniferous-Permian wells is mostly distributed in the Zhanhua sag and Chezheng sag in the north, while in the Dongying and Huimin sags in the south, relatively few wells are drilled in the Carboniferous-Permian coal measures. The distribution limit of the residual carboniferous-Permian strata in this area is controlled by the NE-trending faults developed in the late Mesozoic, which have the characteristics of North-South zoning or subdivision. They mainly distribute along the north-east direction on the slope of each depression to the sag belt. From north to south, they...
are Chexi-Dawang-Chengdong, Shaojia-Luojia-Gubei, Zizhen-Yangxin and Linnan. Lin Fanjia and Dongying Nanpo [26]. The coal-bearing strata of Carboniferous-Permian in Jiyang Depression are buried in depth of 500-7000 m, and the depth in most areas is 2000-6000 m [14]. Residual thickness varies greatly in different locations. For example, the residual thickness in the southern and northern regions is generally 200-800 m and the maximum thickness is 900 m. According to the stratum thickness statistics of single well drilling, Qugu 2 well in Huimin sag has the largest stratum thickness, reaching 845 m, while Yigu 4 well in Zhanhua sag has the smallest stratum, only 9 m. From the distribution of zones, the Chezhen Sag is mostly about 200 m, with the maximum thickness of 642.5 m (Chegu 31 well) and the minimum thickness of 25.5 m (Chegu 11 well) (Figure 2); There are fewer Carboniferous-Permian drillings in Zhanhua sag, with the maximum thickness of 746 m and the minimum of 118 m. In the Dongying Depression, there are few exploration wells in the Carboniferous-Permian, and the distribution is uneven. The maximum drilling thickness is 623 m, and the minimum is 23 m; the maximum drilling thickness in Huimin sag is 845 m and the minimum is 168 m. According to the statistics of the drilled coal seam and the dark mudstone, the thickness of the coal seam is between 14-29 m, and the dark mudstone thickness is about 260 m.

4. Organic Geochemical Characteristics of Mud Shale and Evaluation of Source Rocks

4.1 Abundance of Organic Matter

Organic carbon (TOC) is the basis of hydrocarbon generation, and is also one of the important parameters reflecting the abundance of organic matter in shale [27]. It is also a key parameter for evaluating the source rock’s gas generating capacity and gas production [28]. If the content of organic carbon is high, the ability of shale to generate hydrocarbon is strong, which mean that there are enough parent materials to generate hydrocarbons [29-30]. Hydrocarbon generation potential refers to the maximum amount of organic matter in a unit source rock that is able to be converted into hydrocarbons under natural geological conditions, usually expressed as S1 + S2. S1 indicates hydrocarbons that have been generated but not discharged from rocks, also known as residual hydrocarbons, and S2 indicates organic matter that is able to be generated but has not yet generated hydrocarbons in rocks [31].

4.1.1 Organic Matter Abundance of Benxi Formation and Taiyuan Formation

Most of the mudstones of Benxi and Taiyuan Formations in Dongying Depression have TOC less than 1.5%, S1+S2 less than 0.6 mg/g, and TOC and S1+S2 values in carbonaceous mudstones are higher, HI is 10-100, which generally belongs to poor gas source rocks.

The TOC of shale in Huimin Depression is generally 0.5% ~ 2.5%, and S1+S2 is generally 1 mg/g, up to 14.66 mg/g, generally medium-poor gas source rock. Mudstones in Zhanhua sag are generally moderate to better gas source rocks. TOC in mudstone is generally greater than 1%, S1+S2 is mostly 0.5 ~ 4 mg/g, HI is lower, generally less than 100. Regionally speaking, TOC of Carboniferous in Luojia area is 0.6% ~ 1%, S1+S2 is basically less than 0.5%, and most of them are medium-poor gas source rocks with a Ro of 4% (Table 1). In the Yihezhuang area, the TOC of shale is generally 1% ~ 6%, S1+S2 is generally 1mg/g, the maximum is 15.32mg/g, and the maturity Ro is 0.8 ~ 1.35. It belongs to medium-good Source rock. The TOC of the Carboniferous mudstone in the Gubei area is generally low, ranging from 5% to 8%, and the maturity of Ro is 1.5% to 1.8%. It belongs to better gas source rock. (Table 1).

According to TOC, S1+S2, and HI frequency analysis, the TOC of mudstones in Benxi Formation and Taiyuan Formation is less than 4%, and the concentration distribution range is between 0.6% ~ 4%, which is medium-poor gas source rock (Figure 3). Among them, TOC was mainly 0.6%~1.5%, accounting for 49%, and the maximum peak value was 0.8%. S1+S2 is less than 3 mg/g, accounting for the vast majority, and is evaluated as medium-poor gas source rocks. The peak values of Benxi and Taiyuan Formations are about 0.1 mg/g, while those of Shanxi Formation are slightly better, about 0.6 mg/g. The HI is less than 100, and the medium-good source rock is about 40%. The
overall assessment is medium-poor gas source rock. At the same time, the study also reveals that the mudstones of the Benxi and Taiyuan Formations are generally better in the north than in the south, while Dongying, Huimin, Chezhen and Zhanhua are better in turn (Table 1).

Figure 3. Frequency map of TOC S1+S2 HI of mudstones of Benxi and Taiyuan (a, b, c), Shanxi (d, e, f) Formations in Jiyang Depression

Table 1. Geochemical characteristics of mud shale in Jiyang Depression

<table>
<thead>
<tr>
<th>Position</th>
<th>Region</th>
<th>TOC%</th>
<th>S1+S2mg/g rock</th>
<th>HI</th>
<th>Maturity</th>
<th>Evaluation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Benxi formation and Taiyuan formation</td>
<td>Dongying</td>
<td>&lt;1.5</td>
<td>0.6</td>
<td>10-100</td>
<td>0.7-2.4</td>
<td>poor</td>
</tr>
<tr>
<td></td>
<td>Huimin</td>
<td>0.5-2.5</td>
<td>0.3-1.5</td>
<td>40-60</td>
<td>0.8-2.2</td>
<td>middle-poor</td>
</tr>
<tr>
<td></td>
<td>Zhanhua (Luojia)</td>
<td>0.6-1</td>
<td>&lt;0.5</td>
<td>&lt;40</td>
<td>4%</td>
<td>poor-middle</td>
</tr>
<tr>
<td></td>
<td>Zhanhua (Yizhuang)</td>
<td>1-6</td>
<td>1-15.32</td>
<td>&lt;100</td>
<td>0.8-1.35</td>
<td>middle-well</td>
</tr>
<tr>
<td></td>
<td>Zhanhua (Isolated north)</td>
<td>5-8</td>
<td></td>
<td>1.5-1.8</td>
<td></td>
<td>preferably</td>
</tr>
<tr>
<td>Shangxi formation</td>
<td>Dongying</td>
<td>1.21-30.81</td>
<td>0.51-10.33</td>
<td>&lt;100</td>
<td>1.0</td>
<td>middle-pref erably</td>
</tr>
<tr>
<td></td>
<td>Huimin</td>
<td>0.5-2.5</td>
<td>&lt;1.5</td>
<td>30-60</td>
<td>1.1</td>
<td>middle-poor</td>
</tr>
<tr>
<td></td>
<td>Chezhen</td>
<td></td>
<td>0.9</td>
<td></td>
<td></td>
<td>middle-pref erably</td>
</tr>
<tr>
<td></td>
<td>Zhanhua (Isolated north)</td>
<td>&gt;1</td>
<td>maturity</td>
<td>-</td>
<td></td>
<td>middle-pref erably</td>
</tr>
<tr>
<td></td>
<td>Zhanhua (Isolated north)</td>
<td>0.8-3</td>
<td></td>
<td>middle</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4.1.2 Organic Matter Abundance in Shanxi Formation

Carbonaceous mudstones are developed in Permian in Dongying Depression, with high TOC content ranging from 1.21% to 30.81%. TOC of carbonaceous mudstones is generally greater than 10%. S1+S2 is generally greater than 3 mg/g. Therefore, carbonaceous mudstones of Dongying Depression in Permian is a medium-fine gas source rock. (Table 1).

Permian TOC in Huimin sag is mainly 0.5%~2.5%, accounting for 70%. Grade distribution of effective gas source rocks: TOC mass fraction is less than 0.6%, accounting for 10%; TOC mass fraction is 0.6%~1.5%, accounting for 38%; TOC mass fraction is 1.5%~4.0%, accounting for 43%; TOC mass fraction is more than 4%, accounting for 9%. The hydrocarbon generation potential is mainly less than 1.5 mg/g, accounting for 88%. HI distributes mainly in the range of 30~60. The overall evaluation is medium-poor gas source rock (Table 1).

The Permian mudstones in the Chezhen sag has only been analyzed in Well Da 51, which is a medium-good gas source rock, slightly better than the underlying Carboniferous system (Table 1).

The TOC distribution area in Zhanhua sag is relatively wide, ranging from 0.5% to 6%, and S1+S2 is generally less than 2 mg/g. The evaluation is mainly medium gas source rocks. Each area in Zhanhua sag are different. The TOC of Permian mudstones in the Gubei area is generally more than 1%, with a maximum of 5.19%, and the maturity is also high. The peak temperature of pyrolysis is generally above 450°C and the highest temperature is 540°C. It is in the mature-high maturation stage. So most of them belong to medium-better gas source rocks. Among them, 54% are medium gas source rocks, better gas source rocks account for 15%, and the rest are poor gas source rocks. TOC in Gunan area is 0.8%~3%, which belongs to medium gas source rock (Table 1).

Generally speaking, the regularity of hydrocarbon source rocks in Shanxi Formation is not as good as that in Benxi Formation and Taiyuan Formation. Although medium-good hydrocarbon source rocks is able to be found in each depression, their scope is limited (Table 1).

Through TOC, S1+S2, and HI frequency analysis, it was found that TOC of source rocks in Shanxi Formation is generally less than 4%, and the main distribution range is 0.6%~4%. The peak value ranged from 0.6% to 1.5%, accounting for 37%. The distribution of S1+S2 is generally less than 4 mg/g and concentrated in the range of less than 1 mg/g. Among them, 22% were S1+S2 less than 0.5 mg/g, 43.9% were S1+S2 0.5-1.0 mg/g, and only 34% were others. The distribution of HI is generally less than 100. The proportion of medium-good source rock is about 40%, and that of poor source rock is about 50%. The overall evaluation is medium to poor source rocks.

4.2 Organic Type

Zhang Shanwen et al. [32] found that the whole background of the Bohai Bay Basin in the depositional period of the Benxi and Taiyuan Formations is the organic sedimentary facies of the shallow marsh forest, and that there were nearly East-
West marsh forest sedimentary organic facies in the northern part of Jiyang Depression. During the sedimentary period of the Shanxi Formation, the Bohai Bay Basin developed mainly in the environment of delta, lagoon and tidal flat. The organic facies of shallow marsh forest deposits decreased significantly. The organic facies of terrestrial forest deposits developed in the northern part of Jiyang Depression and the organic facies of terrestrial forest deposits developed in the southern part of Jiyang Depression, while the organic facies of other deposits decreased significantly compared with Taiyuan formation, and the distribution range also decreased significantly. It is able to be concluded that the sedimentary organic facies of the Taiyuan Formation coal is much richer than that of the Shanxi Formation, and the hydrocarbon generation potential of the Taiyuan Formation coal is obviously better than that of the Shanxi Formation. The distribution map of organic elements in Jiyang area has been made. It is able to be found that the main type of organic matter in Carboniferous-Permian source rocks in Jiyang Depression is type III kerogen (Figure 4), which is mainly gas-generating source rocks.

### 4.3 Organic Maturity

The maturity of organic matter plays an important role in shale gas formation. When the maturity is low (Ro < 0.6%), shale gas is mainly biogenic gas, or secondary biogas [33-34], which is formed by the biochemical decomposition of freshwater leaching after shallow burial. Biogenic gas and pyrolysis gas will be formed at the same time, and they are mixed shale gas with high and low maturity. When the maturity is high (1.1% < Ro < 2.0%), the shale gas mainly comes from the pyrolysis of organic matter and hydrocarbons, which is high maturity shale gas. When the thermal evolution degree of shale reaches over mature stage (Ro > 2.0%), shale gas is mainly dry gas of hydrocarbon pyrolysis.

The distribution of organic matter maturity RO of Carboniferous-Permian in Jiyang Depression is quite different, ranging from 0.6% to 5.16%. On the bulge and slope, the maturity of gas source rocks varies significantly among different regions. The Checheng-Dawangzhuang area has the lowest maturity, and the 4000m only reaches mature stage. In some areas, the maturity is high. For example, Gubei in Zhanhua, Luojia and Qudi in Chezhen, the maturation degree is higher, and Ro reach mature-high mature stage, which is related to the depth of burial (Table 2). From a flat point of view, the distribution trends of maturity of the Taiyuan Formation and the Shanxi Formation in the Bohai Bay Basin are consistent (Figure 5 and Figure 6). The Dongying sag is the main body, and the center of Zhanhua sag and Huimin sag are the high maturity centers, which distribute in a circular belt. Dongying sag is mainly in the high mature stage, Zhanhua sag and Huimin sag are mainly in the middle and late mature stage, while the western part is still in the mature stage.

![Figure 4. Organic elements distribution of coal series in Jiyang Depression](image)

**Table 2.** Coal series maturity of Permo-Carboniferous in Jiyang Depression

<table>
<thead>
<tr>
<th>Region</th>
<th>Depth (m)</th>
<th>Ro (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chezhen Dawangzhuang</td>
<td>2000-4000</td>
<td>0.62-0.72</td>
</tr>
<tr>
<td>Zhanhua Yidong</td>
<td>2000</td>
<td>0.63-0.9</td>
</tr>
<tr>
<td>Chezhen Zhuxiangqianshan</td>
<td>3500-4000</td>
<td>0.75-0.84</td>
</tr>
<tr>
<td>Zhanhua Isolated north</td>
<td>3700-5000</td>
<td>0.98-1.77</td>
</tr>
<tr>
<td>Zhanhua Island - Isolated north</td>
<td>2000-3100</td>
<td>0.65-0.87</td>
</tr>
<tr>
<td>Chezhen Luojia</td>
<td>3000-3400</td>
<td>1.18-1.48</td>
</tr>
<tr>
<td>Chezhen Wangpan town</td>
<td>2400-2700</td>
<td>0.75-1.05</td>
</tr>
<tr>
<td>Chezhen Qudi town</td>
<td>2400-3600</td>
<td>0.85-1.3</td>
</tr>
</tbody>
</table>

![Figure 5. Contour line of organic matter maturity of Benxi and Taiyuan Formations](image)
5. Comparison of Hydrocarbon Generation potential of coal-bearing shale gas in Jiyang Depression

5.1 Stratigraphic Distribution Comparison

Compared with the large Carboniferous-Permian coal-forming gas fields (Suqiao-Wenan, Dongpu and Wuqing) discovered in North China, the coal-bearing strata in Jiyang Depression are widely distributed, reaching 8700 km², second only to the Ordos Basin and the southern part of North China, but their stratigraphic continuity is poor. The stratum thickness is 200-800 m and belongs to the medium thickness stratum. Thus, the coal-bearing stratum conforms to the distribution characteristics of the existing Carboniferous-Permian coal-formed gas fields (Table 3).

5.2 Comparison of Shale Distribution and Maturity

The thickness of dark mudstone in Jiyang Depression ranges from 40 m to 100 m, with a maximum of over 300 m, and the thickness varies greatly. Most shales are buried in the depth of 900-8000 m, but generally more than 3000 m, which belongs to the deep buried area. The maturity of shale is 0.6%~1.3%, which is lower than that of Dongpu, southern North China and Ordos Basin, but similar to that of Suqiao-Wenan. In general, the shale in Jiyang Depression is deeply buried, and its maturity is similar to that in other depressions (Table 4).

5.3 Comparison of Shale Abundance

The organic matter abundance of the Carboniferous-Permian mudstones in Jiyang is at a medium level. TOC of shale is 0.5%~30.81%, which is generally greater than 1%. The hydrocarbon generation potential is 0.3-116.09 mg/g. Compared with other basins, the organic carbon content of mudstone in Jiyang Depression is in the middle level, and the hydrocarbon generation potential is relatively high, slightly lower than the Ordos Basin. Therefore, the Jiyang Depression has a certain potential for hydrocarbon generation in shale (Table 5).

### Table 3. Mud shale characteristics of main gas field in our country

<table>
<thead>
<tr>
<th>region</th>
<th>formation thickness (m)</th>
<th>distribution area (km²)</th>
<th>distribution</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jiyang [14]</td>
<td>200-800</td>
<td>8700</td>
<td>part</td>
</tr>
<tr>
<td>Suqiao-Wenan [14]</td>
<td>700-1000</td>
<td>4564</td>
<td>part</td>
</tr>
<tr>
<td>Dongpu [14]</td>
<td>700-1000</td>
<td>5300</td>
<td>part</td>
</tr>
<tr>
<td>Wuqing [14]</td>
<td>2560</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Southern north China [35]</td>
<td>600-900</td>
<td>31000</td>
<td>Part</td>
</tr>
<tr>
<td>Ordos Basin [36]</td>
<td>245800</td>
<td></td>
<td>continuous</td>
</tr>
</tbody>
</table>

### Table 4. Mud shale characteristics of main gas field in our country

<table>
<thead>
<tr>
<th>region</th>
<th>General mud shale thickness (m)</th>
<th>Maximal shale thickness (m)</th>
<th>cover depth (m)</th>
<th>maturity (Ro(%))</th>
<th>Gas reservoir conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jiyang [25]</td>
<td>50-100</td>
<td>300</td>
<td>900-8000</td>
<td>0.6-1.3</td>
<td>gas show</td>
</tr>
<tr>
<td>Suqiao-Wenan [25]</td>
<td>200-400</td>
<td>400</td>
<td>2600-4500</td>
<td>0.5-1.3</td>
<td>proven reserves 209×10⁶ m³</td>
</tr>
<tr>
<td>Dongpu [25]</td>
<td>100-160</td>
<td>1500-6000</td>
<td></td>
<td>0.8-2.0</td>
<td>proven reserves 480×10⁹ m³</td>
</tr>
<tr>
<td>Wuqing [25]</td>
<td>48-284</td>
<td>&gt;3000</td>
<td></td>
<td>0.64-1.06</td>
<td>industrial gas flow</td>
</tr>
<tr>
<td>Southern north China [35]</td>
<td>300-400</td>
<td>600</td>
<td>1000-9000</td>
<td>0.8-3</td>
<td></td>
</tr>
<tr>
<td>Ordos Basin [36]</td>
<td>60-200</td>
<td>200</td>
<td>600-5000</td>
<td>&gt;2.0</td>
<td>Large gas fields</td>
</tr>
</tbody>
</table>

### Table 5. Mudshale characteristics of main gas field in our country

<table>
<thead>
<tr>
<th>region</th>
<th>organic carbon %</th>
<th>HI</th>
<th>S1+S2/(mg.g–1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jiyang [21]</td>
<td>0.5-30.81</td>
<td>30-100</td>
<td>0.3-116.09</td>
</tr>
<tr>
<td>Suqiao-Wenan [25]</td>
<td>0.1-26.9</td>
<td></td>
<td>0.02-77.9</td>
</tr>
<tr>
<td>Dongpu [23]</td>
<td>0.1-39.8</td>
<td></td>
<td>0.17-76.26</td>
</tr>
<tr>
<td>Wuqing [23]</td>
<td>0.1-38.8</td>
<td></td>
<td>0.02-82.06</td>
</tr>
<tr>
<td>Southern north China [35]</td>
<td>0.38-33.93</td>
<td>8.5-223.3</td>
<td>0.1-77.17</td>
</tr>
<tr>
<td>Ordos Basin [36]</td>
<td>0.05-23.38</td>
<td>212-266</td>
<td>94.7-204.1</td>
</tr>
</tbody>
</table>

In summary, compared with the shale characteristics of the main Carboniferous-Permian coal-formed gas fields...
in China, the hydrocarbon generation capacity of the Carboniferous-Permian coal-formed shale in Jiyang Depression is generally at a medium level, slightly higher than that in Puyang and South North China Basins, and has certain shale gas exploration potential.

6. Conclusion

(1) The Carboniferous-Permian residual strata in Jiyang Depression are thinner in the north and thicker in the south. The residual thickness is generally 200-800m, and the drilling thickness is up to 900 m. Due to the impact of the Mesozoic-Cenozoic fracture, the distribution of the Carboniferous-Permian strata in the northern part of Jiyang Depression is more obvious, and mainly distributed along the slopes of the sag to the sub-sag in the NE direction, and is distributed on five regional tectonic belts, from north to south, respectively for Chexi - Dawang - Chengdong, Shaojia - Luojia - Gubei, Zizhen - Yangxin, Linnan - Linfanjia, Dongying South Slope.

(2) Carboniferous-Permian coal rocks belong to better hydrocarbon source rocks. Type III kerogen of organic matter is conducive to gas generation. The maturity of organic matter reaches a mature-higher maturity stage and has the material basis for coal-bed methane generation. There are differences in the hydrocarbon generation potential of mudstones: Benxi Formation and Taiyuan Formation have better hydrocarbon generation potential in the northern part of the basin, that is, Dongying, Huimin, Chezhen and Zhanhua that become better in turn. And the regularity of hydrocarbon source rocks of Shanxi Formation is weaker than that of Benxi Formation and Taiyuan Formation. and medium-good hydrocarbon source rocks is found in each depression. However, the range is limited, and the overall evaluation is still moderate.

(3) Compared with other areas in China, the coal measures in Jiyang Depression are widely distributed and moderately thick. The organic matter abundance of Carboniferous-Permian mudstone is in the middle level, and the Carboniferous-Permian mudstone has certain hydrocarbon generation potential and exploration potential.

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ARTICLE

3D Gravity Inversion with Correlation Image in Space Domain and Application to the Northern Sinai Peninsula

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ABSTRACT

We present a 3D inversion method to recover density distribution from gravity data in space domain. Our method firstly employs 3D correlation image of the vertical gradient of gravity data as a starting model to generate a higher resolution image for inversion. The 3D density distribution is then obtained by inverting the correlation image of gravity data to fit the observed data based on classical inversion method of the steepest descent method. We also perform the effective equivalent storage and subdomain techniques in the starting model calculation, the forward modeling and the inversion procedures, which allow fast computation in space domain with reducing memory consumption but maintaining accuracy. The efficiency and stability of our method is demonstrated on two sets of synthetic data and one set of the Northern Sinai Peninsula gravity data. The inverted 3D density distributions show that high density bodies beneath Risan Aniza and low density bodies exist to the southeast of Risan Aniza at depths between 1~10 and 20 km, which may be originated from hot anomalies in the lower crust. The results show that our inversion method is useful for 3D quantitative interpretation.

1. Introduction

3D gravity inversion is vital to quantitative interpretation of the Earth’s interior compositions and structures. However, gravity inversion is never unique due to the ubiquitous presence of observation errors and the inherent source ambiguity of the gravity potential [⁴⁰]. Numerous imaging methods for potential field data have been proposed to estimate source parameters. Patella [³²] presented a probability inversion method which was applied to gravity data by Mauriello and Patella [¹⁹]. Guo et al. [¹⁴,²⁰] proposed the correlation image method based on the study of probability images, which produced a higher resolution of density/magnetization distribution by using the vertical gradient of potential data. Fedi [⁷,⁸] presented Depth from Extreme Points (DEXP) method and demonstrated that the resulting image was equivalent to a weighted upward continuation of potential fields by comparing with other methods. Baniamerian et al. [³,⁴] proposed a variant of the DEXP method, which generated an image of a quantity proportional to the source distribution. Chauhan et al. [⁶] de-

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scribed an accurate method for performing upward continuation and vertical differentiation in space domain. Because the methods are all noniterative, stable, and convenient in calculation, they are touted as providing useful starting model for 3D inversion.

Forward calculations for potential field are mainly divided into space- and frequency-domains. Space domain methods provide closed-form equations to calculate potential fields directly and accurately. However, when large number of field data is to be modeled, space domain solutions are considerably slow. Frequency domain methods are simpler and faster by using the Fast Fourier Transform, but they have been plagued by imposed periodicity and edge effect (e.g. [3]).

There are two basic methods to partly overcome the problems of the great cost of computational time and memory footprint in the space domain processing and interpretation: (1) fast calculation of forward modeling, and (2) reducing the number of inversion iterations on the basis of maintaining accuracy. Portniaguine and Zhdanov [21,29] proposed a compression technique based on cubic interpolation for decreasing computer memory and accelerating the calculation speed. Li and Oldenburg [16] introduced a wavelet transform to compress the sensitivity matrix and improved the efficiency of forward modeling. Yao [27] presented an equivalent storage technique based on the equivalence and interchangeability of potential field to inverse gravity and magnetic anomalies for 3D physical properties. Yao et al. [28] proposed a stochastic subspace technique to reduce the number of inversion dimensions. Shamsipour et al. [24,25] presented stochastic inversion to reduce the number of inversion iterations. Abedi et al. [2] applied a bidiagonal matrix with favorable lower dimensions to increase the speed of the algorithm. MohammadRezaie et al. [18] combined the Krylov method with a regularization method applied to the low-dimensional projected problem.

In this work, we present a 3D gravity inversion with correlation image in space domain. Firstly, we take the 3D correlation image of the vertical gradient of gravity data (CIVG) as a starting model to generate a smooth image. Secondly, we use effective equivalent storage and subdomain techniques to increase the computational speed of forward modeling. Thirdly, 3D density distributions are obtained by inverting CIVG to fit the synthetic/field data using the steepest descent method. Because the effective equivalent storage and subdomain techniques are utilized to the starting model calculation of the forward modeling and the inversion, all these processes can be carried out fast in space domain with reducing memory consumption but maintaining accuracy. We further verify the feasibility and stability of the method by applying on the field data of the Northern Sinai Peninsula.

2. Methodology

2.1 Gravity Data and Its Vertical Gradient Correlation Image

Guo et al. [10] presented a correlation image method for gravity data and its vertical gradient on regular gridded data. Suppose that the z-axis is positive downwards, and the observation plane is at zero level. The gravity anomaly caused by an arbitrary cell q with volume V can be expressed as

\[
g(x_i, y_i) = GV\Delta \sigma_q \frac{B_q(x_i, y_i)}{r(x_i, y_i)}.
\]

where G is the Newton’s gravitational constant, \(\Delta \sigma_q\) is the density contrast between the anomalous body and background mass, and \(B_q(x_i, y_i)\) is a geometrical function

\[
B_q(x_i, y_i) = \frac{z_q}{r(x_i, y_i)^3},
\]

where \(r(x_i, y_i) = \left[\left(x_{i} - x_q\right)^2 + \left(y_{i} - y_q\right)^2 + z_q^2\right]^{\frac{1}{2}}\), \((x_i, y_i)\) is the observation point at sea level, and \((x_q, y_q, z_q)\) is the source point.

The normalized correlation between the observed and forward data is calculated as follow [10]

\[
C_q(x_i, y_i, z_q) = \frac{\sum_{i=1}^{N} \Delta g(x_i, y_i) \Delta g_q(x_i, y_i)}{\sqrt{\sum_{i=1}^{N} \Delta g^2(x_i, y_i)} \sum_{i=1}^{N} \Delta g^2_q(x_i, y_i)}
\]

\[
= \frac{\sum_{i=1}^{N} \Delta g(x_i, y_i) \Delta g_q(x_i, y_i)}{\sqrt{\sum_{i=1}^{N} \Delta g^2(x_i, y_i)} \sum_{i=1}^{N} \Delta g^2_q(x_i, y_i)}
\]

where \(\Delta g(x_i, y_i)\) is the observation data, \(C_q(x_i, y_i, z_q)\) is the coefficient of normalized correlation, and N is the total number of observation points. If \(\Delta \sigma_q\) is positive, Eq. (3) can be simplified to

\[
C_q(x_i, y_i, z_q) = \frac{\sum_{i=1}^{N} \Delta g(x_i, y_i) B_q(x_i, y_i)}{\sqrt{\sum_{i=1}^{N} \Delta g^2(x_i, y_i)} \sum_{i=1}^{N} B^2_q(x_i, y_i)}
\]

and according to the Cauchy inequality, we can obtain

\[
-1 \leq C_q(x_i, y_i, z_q) \leq 1.
\]

CIVG can also be expressed in the same way.
\[ C_{q,z}(x_q, y_q, z_q) = \frac{\sum_{i=1}^{N} \Delta g_z(x_i, y_i) B_{q,z}(x_i, y_i)}{\sqrt{\sum_{i=1}^{N} \Delta g_z^2(x_i, y_i) \sum_{j=1}^{N} B_{q,y}(x_j, y_j)}}, \]

\[ \text{in which } \Delta g_z(x_i, y_i) \text{ is the vertical gradient of the observation data, and } B_{q,z}(x_i, y_i) \text{ is the vertical gradient of } B_q(x_i, y_i), \text{ which is also a geometrical function} \]

\[ B_{q,z}(x_i, y_i) = \frac{2z_q^2 - (x_i - x_j)^2 - (y_i - y_j)^2}{\left( (x_i - x_j)^2 + (y_i - y_j)^2 + z_q^2 \right)^{3/2}} \]

\[ \text{The correlation image of either the gravity anomaly or the vertical gradient is equivalent to a weighted upward continuation reflecting the density distribution characteristics. Therefore, CIVG is considered as a useful starting model for the subsequent 3D inversion, which can reduce non-uniqueness, uncertainty and the number of iterations.} \]

### 2.2 Equivalent Storage Technique

Yao [27] proposed an equivalent storage technique based on the equivalence of shift and the symmetry reciprocity of potential field (Figure 1). From Eq. (2), we can see that the geometrical function is only determined by the distances from the centers of cells to the observation points, when the sources locating within one layer. Take the first layer as an example, the distance from the first grid of this layer to the first observation point is equal to the distance from an arbitrary grid of the layer to its corresponding observation point (Figure 1a), which can be written as [27]

\[ B_{(1,1)} = B_{(1,2)} = \cdots = B_{(m,1)} = \cdots = B_{(m,n)}, \]

\[ \text{combining Eq. (9) with Eq. (10), we obtain} \]

\[ B_{(i,j)} = B_{(1,i)} = B_{(i,1)} = B_{(i,j)} \]

Figure 1 is the sketch map showing the distances between the source and observation points used for equivalent storage technique. When grid meshing has been suitably established, the geometry of gridding is fixed in the iterative inversion. We can then employ the equivalent storage technique to relax the demand on computer memory and increase the computational efficiency. It is worth mentioning that the technique works when the gridding of 3D domain along the \( X \) - and \( Y \)-directions is the same as that used for the observation plane.

### 2.3 Subdomain Technique

To further increase the computational speed and reduce the memory usage, we propose a technique of subdomain in this section. We calculated the gravity anomaly by an infinitely extended line along the \( X \) -axis with depth \( z_q \). We assume a line segment length \( a \) with density \( \sigma \) in the plane 2(b-a) with density \( k \sigma \), here \( h \) is infinity, and \( k \) is constant. The gravity anomaly above the center of line segment can be expressed as

\[ \Delta g = G \sigma \int_{-a}^{a} \frac{z}{r^2} dx = G \sigma \left[ \int_{-a}^{a} \frac{z}{\sqrt{a^2 + z^2}} dx \right] = G \sigma \left[ \frac{a}{\sqrt{a^2 + z^2}} \right] = G \sigma \left[ \frac{2a}{\sqrt{a^2 + z^2}} \right]. \]

Then the ratio of the gravity anomalies between the whole line and the line segment can be expressed as

\[ \frac{\Delta g_{\text{line}}}{\Delta g_{\text{segment}}} = \frac{G \sigma \int_{-a}^{a} \frac{z}{r^2} dx}{G \sigma \int_{-a}^{a} \frac{z}{\sqrt{a^2 + z^2}} dx} = \frac{G \sigma \left[ \frac{2a}{\sqrt{a^2 + z^2}} \right]}{G \sigma \left[ \frac{a}{\sqrt{a^2 + z^2}} \right]} \]

Based on Eq. (9), the geometrical function of an arbitrary point can be replaced by the first point on the same layer. The interchangeability of the geometrical functions can be written as

\[ \int_{-k}^{k} \frac{z}{r^2} dx = \int_{-k}^{k} \frac{z}{\sqrt{a^2 + z^2}} dx \]

\[ \text{combining Eq. (9) with Eq. (10), we obtain} \]

\[ B_{(i,j)} = B_{(1,i)} = B_{(i,1)} = B_{(i,j)} \]

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Because $b$ is infinity number, we can obtain
\[
\frac{\Delta g_2}{\Delta g_1} = k \frac{b \sqrt{a^2 + z_q^2} - ab}{ab} + 1 = k \left( \sqrt{1 + \left( \frac{z_q}{a} \right)^2} - 1 \right) + 1,
\]
assuming $a = 20z_q$, and $k = 10$, then
\[
\frac{\Delta g_2}{\Delta g_1} = 10 \left( \sqrt{1 + \left( \frac{1}{20} \right)^2} - 1 \right) + 1 = 10 \times 0.001 + 1 = 1.01
\]
\*MERGEFORMAT (14)

Eq. (15) implies that the subdomain technique is an approximate quantitative determination method to reduce the computational time of forward modeling with a high fitting accuracy. Due to the line is arbitrary, and all other lines can be applied in the same layer, this technique can be extended to the entire plane.

Here we take an example to illustrate the efficiency of the combined techniques of equivalent storage and subdomain. A 3D domain is divided into $1000 \times 1000 \times 10$ cubic prisms with a grid spacing of 1, and the observation data are also calculated on a $1000 \times 1000$ grid with an interval of 1. The storage of a geometrical function is $10^{13}$ without using the equivalent storage technique, whereas the storage is $10^7$ if using the equivalent storage technique. With the subdomain technique, the storage can be further reduced to be $10^5$.

### 2.4 The Steepest Descent Inversion Method

The conventional way of solving ill-posed inverse problems is based on the misfit functional determined as a norm of difference between the observed and theoretical data
\[
p(m, d) = \| A(m) - d \| = \min, \ \text{\*MERGEFORMAT (16)}
\]
where, $A$ is the forward modeling operator, $d$ is the observation data.

In this study, we apply the steepest descent method to inverse the 3D density distribution. One iteration step, from iteration number $n$ to number $n+1$, can be summarized as follows
\[
\begin{align*}
    r_n &= A(m_n) - d \\
s_n &= A^T r_n \\
k_n &= \|s_n\| / \|I_n\|^2 \\
m_{n+1} &= m_n - k_n I_n, \ \text{\*MERGEFORMAT (17)}
\end{align*}
\]
where $I_n$ is the steepest descent direction, $k_n$ is the step length in the direction, and $r_n$ is the residual between the observed and theoretical data.

### 2.5 Inversion Strategy

The following is a summary of the inversion strategy we used to apply correlation image theory and effective equivalent storage and subdomain techniques to obtain 3D density distribution (Figure 2):

1. we calculate the geometrical function of the point located in the first row and the first column of the 3D domain using Eqs. (2) and (7);
2. we calculate CIVG as a starting model using Eq. (6) with the effective equivalent storage (Eq. (11)) and subdomain techniques (Eq. (14)) for fast computation;
3. we use the steepest descent method for iteration inversion, containing the effective equivalent storage and subdomain techniques for increasing the computation speed;
4. the final 3D density distribution is obtained after achieving the minimum error or the number of iterations by the steepest descent inversion method;
5. output the results.

### 3. Synthetic Model Test

In this section, we apply our fast inversion strategy on two sets of synthetic data: 1) a prism model, and 2) an interface model. The computational time and root-mean-square error (RMSE) of each modeling and inversion are calculated by a personal computer with 4 GB RAM, 3.10 GHz processor on a 32-bit operating system. No priori geologic information has been used to constrain the inversions for either of the two data sets. Therefore, the density variance is from zero to infinity.

The first model (Model 1) consists of two close prismatic sources (solid lines) with same size. They are buried at a depth of 5 km with a density contrast of 0.1 g/cm$^3$. The 3D domain is divided into $50 \times 50 \times 20$ cubic prisms with a grid spacing of 1 km. We add pseudo-random Gaussian noise to the synthetic data with mean value of zero and standard deviation of 0.03 mGal. The gravity anomaly is calculated on a $50 \times 50$ km$^2$ grid with a grid spacing of 1 km along the $x$- and $y$-directions (Figure 3a).

Figure 3b shows the anomaly calculated by taking a semi-infinite model with density contrast of 0 g/cm$^3$. This is usually used as starting values of density in the inversion when there is no prior information available. Figure 3d and g shows the estimated density distribution after 10 iterations at slices of $z = 1$ km and $y = 25$ km,
respectively. The calculated gravity perfectly matches the observed values with an RMSE of 0.12. The density distributions are mainly concentrated in a shallow subsurface with very small density values. Figure 3c shows the estimated anomaly using our inversion strategy by taking CIVG as a starting model, while Figure 3e and h shows the density distribution of the starting model, and Figure 3f and i show the inverted results after 15 iterations at slices of $z = 1$ km and $y = 25$ km, respectively. It can be seen that the CIVG produces smooth models (Figure 3e and h). The final density distribution generates a clear, sharp, high-quality image, and the density value is close to the actual value (Figure 3f and i).

To further evaluate the computational efficiency of our inversion strategy, we use a more complex base- ment interface model (Model 2) with a density contrast of 0.2 g/cm$^3$ (Figure 4). The 3D domain is divided into 150 $x$ 30 $y$ 10 $z$ cubic prisms with a grid spacing of 1 km along the $x$-, $y$- and $z$-directions. Figure 4a presents the synthetic gravity anomaly and Figure 4b shows the starting model using CIVG at slice of $y = 15$ km. Figure 4c and d shows the estimated anomaly and the inverted result at slice of $y = 15$ km without the subdomain technique. Figure 4e and f shows the estimated anomaly and the inverted result with subdomain technique. The observation anomaly can be fitted using the proposed procedure in this study with or without subdomain technique from comparing Figure 4c and e with Figure 4a. Meanwhile, comparing with Figure 4b, the result of our method (Figure 4d and f) clearly outlines the fluctuation of the interface and enhances the visibility and sharpness of geological structures, and is close to the true interface.

Table 1 shows the statistical information of the two different synthetic models. Form Model 1, although the semi-infinite model can reconstruct the anomaly with fewer iterations, less time than CIVG, the density distribution is quite deviate from the true position and the numerical value is smaller than the actual value. It is worth noting that the small RMSE and good fitting of anomaly do not represent the real underground density distribution, which is the manifestation of multi-solution inversion. Therefore, CIVG is a better choice as a starting model without prior information. Form Model 2, Subdomain technique takes less time and has smaller RMSE with the same number of iterations, comparing between Figure 4d and f. Subdomain technique greatly improves computational efficiency without losing accuracy, the larger the data set, the more efficient our method. It should be pointed out that we can reduce the grid spacing to achieve higher resolution results with the time and memory decreasing by our method.

4. 3D Gravity Inversion of the Northern Sinai Peninsula

In this section, we further apply our 3D inversion method to obtain density distributions of the Northern Sinai Peninsula and compare our density results with previous study \cite{11}. The Sinai Peninsula is located between the Mediterranean and Red seas and is bounded by the Gulf of Suez to the west and the Dead Sea Transform to the east (Figure 5). The study area is a continental block between the African and Arabian plates, and underwent complex tectonics due to the interactions of different tectonic units. During the Late Triassic, the breakup of the north Afro-Arabian plate and the opening of the Tethys reactivated ENE-WSW trending deep faults. As the African plate moved towards to the Eurasian plate, the Tethys Sea began to close during the Late Cretaceous to pre-Miocene times, resulting in a series of NE-ENE oriented doubly plunging folds originated from inversion of the Mesozoic extensional basins in the Northern Sinai Peninsula. These inversion folds connected with the Syrian Arc Fold Belt to the northeast \cite{12,21}. The aim of the present study is to carry out 3D gravity inversion to obtain density distribution of the Northern Sinai Peninsula and to help further understand the major tectonic and geologic characteristics.

The Bouguer gravity anomaly is reproduced in Figure 5a after digitizing the anomaly presented by Khalil et al. \cite{11}. A gravity high is observed at Risan Aniza to the south of EI-Arish, and it decreases gradually to a medium value at Sheikh Zwayed, whereas gravity lows are observed to the southeast of Risan Aniza. Figure 6b shows the residual anomalies based on the method of Abdelrahman et al. \cite{11}. Both Risan Aniza and Sheikh Zwayed show high positive values on the residual Bouger anomaly map, indicating high density bodies underneath these regions. Southeast of Risan Aniza, large area exhibits negative anomalies, implying low densities at depth. In this study, we utilize the inversion strategy proposed in section 2.5 to obtain the 3D density distributions from the residual Bouguer anomalies (Figure 6b).

The inversion domain is divided into $101 \times 113 \times 10$ cubic prisms with a grid spacing of 1 km along the $x$-, $y$- and $z$-directions. The background density value is taken as 2.67 g/cm$^3$, and the minimum and maximum density values are assumed to be 2.2 g/cm$^3$ and 2.9 g/cm$^3$ according to the known geological and geophysical investigations of the study area, respectively. Therefore, the density contrast ranges from -0.47 to 0.23 g/cm$^3$ across the study area.
Figure 7 shows the initial density distributions, which are calculated by the linear superposition of relative densities (calculated from correlation images based on Eq. (6)) and the background density (2.67 g/cm$^3$) at different depths (1, 2, 3, 5, 10 and 20 km). Figure 7a shows the estimated gravity anomaly after 12 iterations, and the computational time and RMSE are 21 s and 0.19, respectively. The fitting errors, which are the differences between the residual and estimated data, are shown in Figure 8b.

Figure 9 shows the final density distributions at the corresponding depths. Although the final density maps are very similar with the initial density images (Figure 7), there are big differences in the values of density. Our final density distribution model shows distinct high values beneath Risan Aniza at all depth slices (Figure 9). High density bodies are also observed under Sheikh Zwayed at depths between 3 and 20 km. It is interesting that the region to the southeast of Risan Aniza exhibits a slight high density anomaly below 5 km and an evident low density anomaly between 10 and 20 km. Li et al. [13] presented relatively small Curie depths in the same region, indicating a thermal anomaly at depth, therefore resulting in low density bodies to the southeast of Risan Aniza. Based on the horizontal slices, we suggest that there are two deep regional NE-SW trending faults around the high-density contrasts in the northern and southern edges of the Risan Aniza fold zone. We also build a density profile AA1 across El Arish and Risan Aniza (Figure 9g), which shows medium and high density bodies beneath these two regions, respectively. To the southeast of Risan Aniza, the density distribution changes distinctly from low to high anomalies at depth, which may be caused by hot materials in the lower crust.

5. Conclusions

In this paper, we present a 3D gravity inversion method based on correlation image to recover density distributions in space domain. Our method applies CIVG as a starting model to generate a higher resolution image. In addition to the effective equivalent storage, we propose the subdomain techniques for fast calculation of the forward modeling and correlation image, which can reduce the consumption of memory without losing accuracy. We verify the feasibility and stability of our method by testing on both the synthetic and field data. High densities are observed beneath Risan Aniza, whereas low densities exist to the southeast of Risan Aniza at depths between 10 and 20 km, which may be resulted from hot anomalies in the lower crust.

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Supplements

Table 1. Statistical information of two different synthetic models

<table>
<thead>
<tr>
<th>Model</th>
<th>Starting model</th>
<th>Subdomain technique</th>
<th>Iterations</th>
<th>RMSE</th>
<th>Computation time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model 1</td>
<td>Semi-infinite</td>
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<td>10</td>
<td>0.12</td>
<td>22</td>
</tr>
<tr>
<td>Model 1</td>
<td>CIVG*</td>
<td>NO</td>
<td>15</td>
<td>0.12</td>
<td>44</td>
</tr>
<tr>
<td>Model 2</td>
<td>CIVG</td>
<td>NO</td>
<td>16</td>
<td>0.45</td>
<td>63</td>
</tr>
<tr>
<td>Model 2</td>
<td>CIVG</td>
<td>YES</td>
<td>16</td>
<td>0.32</td>
<td>46</td>
</tr>
</tbody>
</table>

Note: *CIVG is 3D correlation image of the vertical gradient of gravity data.

Figure 1. Illustration of the equivalent storage technique

Note: (a) equivalence of shift, and (b) symmetry reciprocation. $B_{i,j,1}(i,j)$ is the geometrical function of Eq. (2), the subscript $(i, j, 1)$ is the source point, and $(i, j)$ is the observation point at sea level.
Figure 2. Flow chart of 3D gravity inversion with CIVG in space domain

Figure 3. Synthetic tests on the prism model

Note: (a) theoretical gravity anomaly, (b) gravity anomaly calculated by taking the density contrast as 0 g/cm$^3$ based on a semi-infinite model, (c) estimated density distribution from the semi-infinite model with density contrast of 0 g/cm$^3$ at slice of $z=1$ km, (d) density distribution of starting model at slice of $z=10$ km, (e) estimated density distribution from the semi-infinite model at slice of $y=25$ km, (f) density distribution of the starting model at slice of $y=25$ km, and (i) inverted result at slice of $y=25$ km. The black lines are the boundaries of the synthetic models.

Figure 4. Synthetic tests on the interface model

Note: (a) theoretical gravity anomaly, (b) the starting model using CIVG at slice of $y=15$ km, (c) estimated gravity anomaly without subdomain technique, (d) inverted result without subdomain technique at slice of $y=15$ km, (e) estimated gravity anomaly with subdomain technique, and (f) inverted result with subdomain technique at slice of $y=15$ km. The black lines are the boundaries of the synthetic models.

Figure 5. Topographic map of the study area. The inset shows the regional tectonic map of the Sinai and the neighboring area.
Figure 6. (a) Digitized Bouguer gravity anomaly of the Northern Sinai Peninsula \cite{11}. The black line is the location of density profile AA1 for Figure 9g. (b) Residual Bouguer gravity anomaly of the Northern Sinai Peninsula

Figure 7. Initial density models at different depths of (a) 1km, (b) 2 km, (c) 3 km, (d) 5 km, (e) 10 km and (f) 20 km

Figure 8. (a) Estimated gravity anomaly after 12 iterations and (b) differences between the residual and estimated gravity data

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Figure 9. Estimated density distributions at different depths of (a) 1 km, (b) 2 km, (c) 3 km, (d) 5 km and (e) 10 km and (f) 20 km, and (g) is the density distribution profile AA1 according to Figure 6a

References


REVIEW

Review of Proposed Stress-dilatancy Relationships and Plastic Potential Functions for Uncemented and Cemented Sands

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ABSTRACT

Stress-dilatancy relationship or plastic potential function are crucial components of every elastoplastic constitutive model developed for sand or cemented sand. This is because the associated flow rule usually does not produce acceptable outcomes for sand or cemented sand. Many formulas have been introduced based on the experimental observations in conventional and advanced plasticity models in order to capture ratio of plastic volumetric strain increment to plastic deviatoric strain increment (i.e. dilatancy rate). Lack of an article that gathers these formulas is clear in the literature. Thus, this paper is an attempt to summarize plastic potentials and specially stress-dilatancy relations so far proposed for constitutive modelling of cohesionless and cemented sands. Stress-dilatancy relation is usually not the same under compression and extension conditions. Furthermore, it may also be different under loading and unloading conditions. Therefore, the focus in this paper mainly places on the proposed stress-dilatancy relations for compressive monotonic loading. Moreover because plastic potential function can be calculated by integration of stress-dilatancy relationship, more weight is allocated to stress-dilatancy relationship in this research.

1. Introduction

Variations of soil and rock volume may be caused by changes in the stress and deformation (mechanical effects) and changes in the water content, the temperature and other reasons (non-mechanical effects) [54]. The tendency of soil or rock to change volume while shearing is called dilatancy [18]. Dilatancy of sand and cemented sand is a crucial phenomenon which differentiates their plastic response from that of metal. That is, dilatancy is one of features of sand and cemented sand that can not be simulated appropriately by the traditional plasticity developed initially for metals. Usefulness of any elastoplastic constitutive model of sand or cemented sand may highly depends on successful implementation of dilatancy response. It is clear that loose sands or weakly cemented sands tend to develop positive pore pressure under undrained shear or to decrease volume under drained shear conditions. Conversely, dense sands and cemented sands tend to develop negative pore pressure in the course of shear or to increase in volume under drained shear conditions [7]. That is, dense sands dilate as deviator stress increases until failure while loose sands decreases in volume with progress of shear loading until failure. This is why dilatancy theory is normally discussed in the context of dense sands. However there is

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usually nothing in proposed stress-dilatancy relations that limit their application to dense sands. Note that in loose sands or weakly cemented sands, zero dilatancy takes places at large strains, but in dense sands, it happens twice during shearing: once temporary at phase transformation when response changes from contractive to dilative, and once at large strains when shearing continues at constant volume.

The geotechnical literature uses the terms dilation and dilatancy interchangeably as we did in the last paragraphs. They are usually stated as an angle compared to friction angle. However, we can divide these two dilatancy definitions into two categories: 1) absolute definition: dilation is the volumetric strain change occurred since the initial condition 2) rate definition: dilation is the ratio of volume change increment relative to shear strain increment. We use the rate definition of dilation in next sections.

Note that the stress-dilatancy equations and plastic potential functions are used extensively in this article. The plastic potential defines the direction of plastic strain increments. The plastic potential is usually expressed using a stress-dilatancy equation which relates the dilatancy rate to the stress ratio.

2. Background

According to the classical plasticity, there exist a plastic potential function such that normal to the function shows components of plastic strain increment. This is to say:

\[
\dot{\varepsilon}_{ij}^p = \lambda \frac{\partial G}{\partial \sigma_{ij}}
\]

where \(\dot{\varepsilon}_{ij}^p\) is plastic strain increment tensor, \(G\) is plastic potential function, \(\sigma_{ij}\) is stress tensor and \(\lambda\) is plasticity multiplier which is calculated using consistency condition.

This rule is called flow rule. Flow rule implies that the derivative of the plastic potential function is important in constitutive modelling rather than the function itself.

Stress-dilatancy relationship in triaxial space also is usually expressed as follows:

\[
d = \frac{\dot{\varepsilon}_{p}^p}{\dot{\varepsilon}_{q}^q} = \frac{\partial G}{\partial q}
\]

where \(d\) is the dilatancy rate, \(\dot{\varepsilon}_{p}^p\) and \(\dot{\varepsilon}_{q}^q\) are volumetric and deviatoric plastic strain increments accordingly, \(p\) and \(q\) are mean effective stress and deviator stress, respectively.

Analysis of direct shear box test of sand by Taylor implies that input work is entirely dissipated in friction. Therefore, we can equal plastic input work to the dissipated energy in friction for triaxial conditions as follows:

\[
p \dot{\varepsilon}_{p}^p + q \dot{\varepsilon}_{q}^q = \frac{M p \dot{\varepsilon}_{p}^p}{q_{\varepsilon}^p} \quad \text{for triaxial compression}
\]

\[
p \dot{\varepsilon}_{p}^p + q \dot{\varepsilon}_{q}^q = -\frac{M p \dot{\varepsilon}_{p}^p}{q_{\varepsilon}^q} \quad \text{for triaxial extension}
\]

\(M\) denotes the slope of critical state line in \(p' - q\) space.

Arrangement of equation (3) gives rise to a very fundamental form of dilatancy equation as follows:

\[
d = \frac{\dot{\varepsilon}_{p}^p}{\dot{\varepsilon}_{q}^q} = \begin{cases} M - \eta & \text{for compression} \\ -M - \eta & \text{for extension} \end{cases}
\]

\(\eta\) is stress ratio which is defined as \(q/p\).

Different values of \(M\) are used for triaxial compression and triaxial extension as follows:

\[
M = \begin{cases} \frac{6 \sin \phi_{cv}}{3 - \sin \phi_{cv}} & \text{for compression} \\ \frac{6 \sin \phi_{cv}}{3 + \sin \phi_{cv}} & \text{for extension} \end{cases}
\]

\(\phi_{cv}\) is the constant volume (critical state) friction angle.

From the above equation, it can be realized that \(M\) (the critical state stress ratio) for compression is greater than \(M\) for extension if the critical state friction angle is the same for both compression and extension.

In order to arrive in better match for experimental observations, a constant \(A\) is often introduced in equation (4) in the following form:

\[
d = \frac{\dot{\varepsilon}_{p}^p}{\dot{\varepsilon}_{q}^q} = A(M - \eta)
\]

\(A\) is a material parameter which may be different for triaxial compression and extension loading and \(\eta\) is current stress ratio. \(A\) should be determined by curve fitting of equation (6) against total volume change.

Equation (4) can also be written in the form of equation (7) as follows:

\[
d = \frac{\dot{\varepsilon}_{p}^p}{\dot{\varepsilon}_{q}^q} = (M - \beta \eta)
\]

\(\beta\) is a constant.
Rowe \cite{47} derived the stress-dilatancy relation for soils using minimum energy consideration for particle sliding as follows\cite{4,41}:

\[
\frac{\sigma'_1}{\sigma'_3} = K \left(1 - \frac{\varepsilon_Y}{\varepsilon_1}\right) \quad \text{for compression} \tag{8}
\]

\[
\frac{\sigma'_1}{\sigma'_3} = \frac{K}{\left(1 - \frac{\varepsilon_Y}{\varepsilon_1}\right)} \quad \text{for extension} \tag{9}
\]

where \(K\) is a parameter which depends on the failure friction angle.

With presuming a constant failure friction angle and neglecting elastic strains, Wood \cite{66} formulated Rowe’s stress-dilatancy relation as follows \cite{15,62,41}:

\[
\begin{cases}
    \{d = \frac{\varepsilon_Y^p}{\varepsilon_Y^q} = \frac{9(M_c - \eta)}{9 + 3M_c - 2M_c\eta} \quad \text{for compression} \\
    \{d = \frac{\varepsilon_Y^p}{\varepsilon_Y^q} = \frac{9(M_c - \eta)}{9 - 3M_c - 2M_c\eta} \quad \text{for extension}
\end{cases} \tag{10}
\]

where \(M_c\) and \(M_e\) are critical state stress ratio in triaxial compression and extension, respectively.

In addition to the constant critical state stress ratio, the variable phase transformation stress ratio (i.e. \(M_{PT}\)) \cite{16,42,43} and the failure stress ratio (i.e. \(M_f\)) have been used in equations (4), (6) and (10) as well. \(M_{PT}\) is a value corresponding to a temporary zero dilatancy which is calculated similar to equation (5) with replacement of the critical state friction angle by the phase transformation friction angle \cite{6,69}. \(M_f\) also is not constant and evolves towards the critical state stress ratio with plastic shearing \cite{4,16}. Replacement of the critical state stress ratio with \(M_{PT}\) or \(M_f\) is performed in order to account for the effect of pressure and density dependency of the stress-dilatancy relationship of sands \cite{15}.

3. Stress-dilatancy Relationships and Plastic Potential Functions

3.1 Cohesionless Sands

Proposed stress-dilatancy relationships and plastic potential functions are presented in a historical sequence. Most of formulas which are presented here are stress-dilatancy relationships. However, some proposed constitutive models have used a plastic potential function to define the direction of plastic flow as well. A summary of these stress-dilatancy relationships and plastic potential functions of uncemented sands with striking highlights is given in table 3 (see appendix section).

(1) Nova and Wood \cite{35}:
Nova and Wood \cite{35} used the following equation as their stress-dilatancy relationship:

\[
d = \frac{M - \eta}{\mu} \tag{11}
\]

where \(M\) and \(\mu\) are positive constants and \(d\) is the dilatancy rate. At critical state, \(\eta=M\) and hence dilatancy rate becomes zero which implies no volume change at the critical state. \((-1/\mu\) is the slope of the linear relation between \(\varepsilon_Y^p/\varepsilon_Y^q\) and \(\eta\).

Cui and Delage \cite{8} applied the same equation as above in their constitutive model.

Plastic potential function associated with this stress-dilatancy relationship is as follows:

\[
g(p',q) = q - \frac{Mp}{1 - \mu} \left[1 - \mu \left(\frac{p}{p_{ug}}\right)^{(1-\mu)/\mu}\right] \quad \tag{12}
\]

where \(p_{ug}\) is value of the isotropic pressure when \(\eta=M\). Note that when \(\mu=1\), the equation reduces to that of the Cam Clay model.

(2) Nova and Wood \cite{36}:
One of the oldest and most popular stress-dilatancy relationships proposed for cohesionless sands was first suggested by Nova and Wood \cite{36}. It was formulated as follows:

\[
d = \left(1 + a_g\right)(M - \eta) \tag{13}
\]

where \(\eta=q/p\) is stress ratio, \(M\) is the critical state stress ratio and \(a_g\) is a material parameter.

Similar stress-dilatancy relationships were used by Pastor et al. \cite{37}, Haeri and Hamidi \cite{13}, Hamidi and Yarbakhti \cite{14} and Kong et al. \cite{25}.

The above relationship results in the following plastic potential function:

\[
g(p',q) = q - Mp'\left(1 + \frac{1}{a_g}\right)\left[1 - \left(\frac{p'}{p_{g}'}\right)^{a_g}\right] \quad \tag{14}
\]

where \(p_{g}'\) is a size parameter which determines size of the plastic potential function.

(3) Jeffries \cite{17}:
Jeffries \cite{17} used the below relationship in his critical state constitutive model to represent the stress-dilatancy behavior. It appears that the formula was proposed based on Nova and Wood \cite{35}'s relation as follows:
where \( N \) is a material parameter and \( d \) is the dilatancy rate which is defined as plastic volumetric strain increment to plastic deviatoric strain increment.

If \( N=0 \) then the above equation reduces to the familiar Cam Clay model. Note that Andrade \[2\] used the same flow rule in his constitutive model.

Jefferies obtained the plastic potential function by integration of his stress-dilatancy relationship and then considered the yield function equals to the plastic potential function (associated flow rule).

Jefferies stated that their stress-dilatancy relationship and constitutive model in general capture the influence of void ratio and mean effective stress on sand response but neglect the influence of fabric (i.e. grain contact arrangement or geometrical packing of particles). He also claimed that the bedding direction during sample preparation pronouncedly affects stress-dilatancy relationship.

Jefferies suggested in his model that an infinite number of isotropic consolidation lines exist for sands which prevents the direct coupling of the yield surface size to the void ratio. This was a novelty in his model which resulted in change of focus from the normally consolidation line to the critical state line in definition of the hardening law. That is, he applied a shear hardening law instead of a volumetric hardening law.

(4) Lagioia et al. \[27\].

Lagioia et al. \[27\] proposed their stress-dilatancy relationship such that the proposed formula fulfills the two following requisites:

\[
\begin{align*}
\eta &\to 0 \implies d \to \infty \\
\eta &\to M \implies d = 0 \\
\end{align*}
\]

This implies that when a material is sheared isotropically \((\eta=0)\), only plastic volumetric strain occurs and also when the stress ratio reaches the critical state value of \( M \) in compressive loading, the critical state condition must meet \[27\]. The following stress-dilatancy relation satisfies the two aforementioned conditions:

\[
d = \mu_g (M - \eta) \left( \frac{\alpha M}{\eta} + 1 \right)
\]  (17)

\( \alpha \) and \( \mu_g \) are model constants. \( \eta \) is the current stress ratio and \( M \) is critical state stress ratio which is defined based on equation (5).

(5) Yu \[71\].

Yu \[71\] used the well-known Rowe’s stress-dilatancy relationship (equation (10)) in his proposed constitutive model named CASM to relate stress ratio and dilatancy rate. Yu \[71\] stated that despite immense effort to develop a better stress-dilatancy relation for sands compared to Rowe’s original or modified relationship, little progress appears to have been made in this area. Based on Rowe’s stress-dilatancy relation, Yu \[71\] and Yu et al. \[72\] obtained the following relation for the plastic potential of sands and clays:

\[
g\left(p',q\right) = 3M(3\ln p' - \ln \phi'_m) + (3 + 2M)\ln \left( \frac{3p' + 2q}{p} \right) - (3 - M)\ln \left( \frac{3p - q}{p} \right)
\]  (18)

The size parameter \( \beta_g \) is a dummy parameter as only the derivative of the plastic potential function with respect to \( p \) and \( q \) is important.

Note that the adopted stress-dilatancy relation in CASM is non-associated flow rule as the plastic potential function is not the same as the proposed yield function in this model.

(6) Schanz et al. \[15\].

Schanz et al. \[15\] used the following equations as the flow rule:

\[
sin \Psi_m = \frac{sin \phi_m - sin \phi_{cv}}{1 - sin \phi_m sin \phi_{cv}}
\]  (19)

where \( \Psi_m \) is the mobilized dilatancy angle, \( \phi_m \) is the mobilized friction angle and \( \phi_{cv} \) is the critical state friction angle which is a material constant. \( \phi_m \) is calculated by below equation:

\[
sin \phi_m = \frac{\sigma'_1 - \sigma'_3}{\sigma'_1 + \sigma'_3 - 2\text{coth} \cdot \cot \phi_p}
\]  (20)

where \( \phi_p \) is the failure friction angle. This equation can easily be proved by shape of a Mohr-Coulomb failure envelope.

The above equations correspond to the famous Rowe’s stress-dilatancy theory \[15\].

Note that the critical state dilation angle can be calculated by the failure friction and dilatation angles as follows:

\[
sin \psi_{cv} = \frac{sin \phi_p - sin \psi_p}{1 - sin \phi_p sin \psi_p}
\]  (21)
The above definition of the flow rule is equivalent to the definition of the plastic potential function in the form of below equation \[^15\]:

\[
g = \frac{(\sigma^1 - \sigma^3)}{2} - \frac{(\sigma^1 + \sigma_3)}{2} \sin \psi_m \tag{22}
\]

(7) Wan and Guo \[^61\]:

Wan and Guo \[^61\] presented a fabric dependent stress-dilatancy equation as follows:

\[
d = \frac{-4}{3} \frac{(\sin \varphi_m - \sin \varphi_f)}{(1 - \sin \varphi_f \sin \varphi_m)} \tag{23}
\]

Depending on magnitude of the characteristic friction angle (\(\varphi_c\)) relative to that of the mobilized friction angle (\(\varphi_m\)), the dilatancy rate changes its sign. This enables the model to capture the change in volumetric response from contractive to dilative which usually observed in dense sands experimentally.

The characteristic and mobilized friction angle in this model are defined as follows:

\[
\sin \varphi_f = -\frac{x}{a} \left(\frac{F_{11}}{F_{33}} + \gamma^{pr} \right) \left(\frac{e}{e_{cr}}\right)^a \sin \varphi_{cr} \tag{24}
\]

where \(F_{11}\) and \(F_{33}\) are fabric tensor components in the axial and radial directions, respectively, \(\gamma^{pr}\) is the true shear strain, \(X\), \(a\) and \(e\) are material constants. \(e\) is the current void ratio and \(e_{cr}\) is the critical state void ratio.

\[
\sin \varphi_m = \frac{\gamma^{pr}}{a + \gamma^{pr}} \left(\frac{e}{e_{cr}}\right)^{-\beta} \sin \varphi_{cr} \tag{25}
\]

where \(\beta\) is a material parameter.

(8) McDowell \[^31\]:

McDowell \[^31\] proposed the following stress-dilatancy relation for sand in his constitutive model:

\[
d = \frac{M^{b+1} - \eta^{b+1}}{\eta^b} \tag{26}
\]

where \(d\) is dilatancy ratio, \(\eta = q/p\) is current stress ratio and \(M\) is the critical state stress ratio and \(b\) is a material parameter.

The plastic potential associated with this stress-dilatancy equation is defined as follows:

\[
g(p', q) = \eta - M \left[(b + 1) \ln \left(\frac{p_0'}{p}\right)\right]^{1/(b+1)} \tag{27}
\]

\(p_0'\) is the value of \(p\) at \(q = 0\).

McDowell’s stress dilatancy equation fulfills the necessary conditions of zero shear strain under isotropic conditions \((\eta = 0 \rightarrow \varepsilon_p^0 = 0 \rightarrow d = \infty)\) and infinite shear strain with zero volumetric strain at the critical state \((\eta = M \rightarrow \varepsilon_p^0 = \infty \& \varepsilon_p = 0 \rightarrow d = 0)\). This approach is identical to that suggested by Lagioia et al. \[^27\].

(9) Russell and Khalili \[^48\]:

Russell and Khalili \[^48\] used the following equation as the streee-dilatancy relation:

\[
d = M_f - \eta = (1 + k_d \zeta) - \eta \tag{28}
\]

where \(k_d\) is a material parameter and \(\zeta\) is the state parameter.

\(M_f\) is used in above equation instead of \(M\) to capture the dependency of \(d\) on density and confining pressure through \(k_d\) and \(\zeta\).

Russell and Khalili \[^48\]’s model was developed in a critical state framework. Certain features of the model are linked to the state parameter \(\zeta\), which is a dimensionless parameter defined as the vertical distance between the current state and the critical state line in the \(e - p\) plane. The state parameter is positive on the loose (wet) side of the critical state line (CSL) and negative on the dense (dry) side of CSL, and expressed as:

\[
\zeta = e - e_{cs} \tag{29}
\]

where \(e\) is the void ratio at the current stress state \((p)\), and \(e_{cs}\) the void ratio at the critical state corresponding to \(p\).

(10) Been and Jefferies \[^4\]:

Been and Jefferies \[^4\] summarized the existing stress-dilatancy relations according to the table 1 and table 2:

<table>
<thead>
<tr>
<th>Theory</th>
<th>Relationship</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cam Clay</td>
<td>(d = (M_f - \eta))</td>
</tr>
<tr>
<td>Modified Cam Clay</td>
<td>(d = (M_f - \eta)/(1-N))</td>
</tr>
<tr>
<td>Jefferies [^17]</td>
<td>(d = d(M_f - \eta)/(1-N))</td>
</tr>
<tr>
<td>Li and Dafalias [^29]</td>
<td>(d = d(M_f - \eta)/(1-N))</td>
</tr>
<tr>
<td>Rowe [^30]</td>
<td>(d = \zeta(M_f - \eta)/(\zeta M_f - 2M_f \eta))</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Authors</th>
<th>Relationship</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Manzari and Dafalias [^33]</td>
<td>(M_f = M + m_d \zeta)</td>
<td>(\zeta) is the state parameter.</td>
</tr>
<tr>
<td>Authors</td>
<td>Equation</td>
<td></td>
</tr>
<tr>
<td>--------</td>
<td>----------</td>
<td></td>
</tr>
<tr>
<td>Li and Dafalias</td>
<td>$M_f = M_{\exp}(m\xi)$</td>
<td>$\xi$ is the state parameter.</td>
</tr>
<tr>
<td>Jefferies and Schuttle</td>
<td>$M_f = M_{\xi}^\xi$</td>
<td></td>
</tr>
<tr>
<td>Wang et al.</td>
<td>$M_f = M_{\xi} + (M - M_f)\xi$</td>
<td>$\xi = \ln(\xi)$</td>
</tr>
</tbody>
</table>

**Note:** $\lambda$ is slope of the critical state line. $m$ and $M_f$ are positive model constants.

(11) Dafalias and Manzari \[33\]:

Dafalias and Manzari \[33\] proposed their stress-dilatancy equation based on difference between the current stress ratio $\eta$ and the dilatancy stress ratio $M_{PT}$ which is known as the phase transformation stress ratio. The suggested relationship is as follow:

$$d = A_d(M_{PT} - \eta)$$

where $A_d$ is material parameter.

For dense sands under small shear strains, $\eta < M_{PT}$ which leads to $d > 0$ (compressive behavior). However, with progress of loading, $\eta$ becomes equal to $M_{PT}$ at a point which results in $d=0$ (temporary steady state response). Further shearing leads to $\eta > M_{PT}$ which results in $d < 0$ (dilatative behavior). Ultimately, the phase transformation stress ratio becomes equal to the current stress ratio at the critical state which leads to zero dilatancy rate (permanent steady state response). Note that the phase transformation state is never reached during shearing of loose sands and $\eta$ is always smaller than $M_{PT}$ leading to prediction of permanent contraction during shearing.

Dafalias and Manzari made $A_d$ fabric dependent. To avoid lengthy discussion, fabric dependency of the stress-dilatancy relationship is not discussed here. Interested reader is referred to Dafalias and Manzari \[33\].

(12) Khalili et al. \[23\]:

The stress-dilatancy equation which was proposed by Khalili et al. \[23\] is similar to that of Russell and Khalili \[48\]. The proposed relation is as follows:

$$d = M_f - \eta = (1 + k_d\xi)M - \eta$$

where $k_d$ is a material constant, $\xi$ is the state parameter and $M$ is the critical state stress ratio.

The variable $M_f$ is used in place of the constant $M$ to account for the dependency of $d$ on void ratio (or density).

Integration of the above stress-dilatancy relation with respect to $p$ and $q$ results in the following plastic potential function:

$$g(p', q, p_0) = q + (1 + k_d\xi)Mp'\ln\frac{p'}{p_0}$$

As mentioned already $\xi$ is a dimensionless parameter defined as the vertical distance between the current state and the critical state line in the $v$ vs. $\ln p$ plane. It is expressed as:

$$\xi = v - v_{cs}$$

where $v=1+e$ is the specific volume at the current stress state ($p$), $e$ is the void ratio, and $v_{cs}$ is the specific volume at the critical state corresponding to $p$.

(13) Imam et al. \[16\]:

Imam et al. presented their stress-dilatancy relation based on concept of the phase transformation stress ratio $M_{PT}$ as follows:

$$d = A(M_{PT} - \eta)$$

$A$ is calculated for triaxial compression and triaxial extension, respectively, as follows:

$$A_c = \frac{9}{9 + 3M_{PT,c} - 2M_{PT,c}\eta}$$

$$A_e = \frac{9}{9 - 3M_{PT,c} - 2M_{PT,c}\eta}$$

where

$$M_{PT,c} = \frac{6\sin\varphi_{PT,c}}{3 - \sin\varphi_{PT,c}}$$

$$M_{PT,e} = \frac{6\sin\varphi_{PT,e}}{3 + \sin\varphi_{PT,e}}$$

and

$$\sin\varphi_{PT,c} = \sin\varphi_{cs} + k_{PT}\xi$$

$$\sin\varphi_{PT,e} = \sin\varphi_{cs} + k_{PT}\xi + a_{PT}$$

where $k_{PT}$ and $a_{PT}$ are material parameters, $\varphi_{cs}$ is the critical state friction angle, $\varphi_{PT}$ is the phase transformation friction angle, $M_{PT}$ is the phase transformation stress ratio and $\xi$ is the state parameter.

The plastic potential function associated with the above flow rule is obtained by the following relationship:

$$g(p', q) = \eta - M_{PT} \left(\frac{A}{A - 1}\right) \left[1 - \left(\frac{p'}{p_0}\right)^{A - 1}\right]$$

for $A \neq 1$

in which $p_0'$ is a measure of the size of the plastic potential function.
The same stress-dilatancy equation was used by Tasiopoulou and Gerolymos [56] in their model. They, however, assigned a value of one for $A$.

(14) Ling and Yang [30]:
Ling and Yang [30] used a combination of work of Nova and Wood [56] and Li and Dafalias [29] to define their stress-dilatancy relation as follows:

$$d = (1 + \alpha_g)(M_f - \eta)$$  \hspace{1cm} (39)$$

$$M_f = M \exp (m\xi)$$  \hspace{1cm} (40)$$

where $\alpha_g$ and $m$ are positive constants and $\xi$ is the state parameter. $\alpha_g$ and $m$ can be determined using the volumetric strain vs. deviator strain curve.

The difference between the above equation with that of Nova and Wood is that a variable stress ratio $M_f$ (which changes with the void ratio and mean effective stress) has been used rather than the constant critical state stress ratio $M$.

The state parameter at the phase transformation for dense sands temporary becomes zero which enables the constitutive model to capture the phase transformation state. However for loose sands, the void ratio is always greater than the critical state void ratio which leads to a positive state parameter. The net result is that $M_f$ is always greater than the current stress ratio which implies that the dilatancy rate is always positive for loose sands (i.e. permanent contractive behavior) except at the critical state in which the dilatancy rate becomes zero. This implies that no volume change occurs at the critical state neither for loose sands nor dense sands because at the critical state, the state parameter is zero which leads to $M_f = M = \eta$.

Liu et al. [32] considered the similar stress-dilatancy equation in their model. However, they replaced $M_f$ with the phase transformation stress ratio.

(15) Sasiharan [49]:
Sasiharan [49] suggested the following stress-dilatancy equation in his anisotropic sand model:

$$d = \frac{M^2 \alpha_g^2 - \eta^2}{2(\eta - \alpha_g)}$$  \hspace{1cm} (41)$$

where $\alpha_g$ is fabric anisotropy parameter which is defined according to the following formula:

$$\alpha_g = \left(\frac{e}{1 + e}\right)^{\beta}$$  \hspace{1cm} (42)$$

in which $e$ is current void ratio and $\beta$ is a material parameter. Thus, the fabric anisotropy parameter evolves with the void ratio.

The plastic potential function corresponds to the above stress-dilatancy relationship is as follows:

$$g(p', q) = \frac{p'}{p} - \frac{M^2}{M^2 + (\eta - \alpha_g)^2}$$  \hspace{1cm} (43)$$

where $p_{cg}$ is the value of $p$ when $\eta = \alpha_g$.

Similar to Jefferies’s approach and conventional Cam Clay model, Sasiharan considered the resulting plastic potential function, obtained by integration of the flow rule, identical to the yield function.

If the fabric anisotropy parameter $\alpha_g$ is zero, the yield and plastic potential surfaces will be an ellipse that is centered along the $p$ axis as in modified Cam Clay model. Sasiharan [49] stated that the above stress-dilatancy relation is not appropriate for anisotropic sands and suggested the following flow rule instead:

$$d = \frac{M^2 - (\eta - \alpha_g)^2}{2(\eta - \alpha_g)}$$  \hspace{1cm} (44)$$

$$\eta = (M^2 + \alpha_g^2)^{\frac{1}{2}}$$ for the first flow rule and $\eta = \pm M + \alpha_g$ for the second flow rule constitute the phase transformation line (i.e. zero dilatancy line) on which zero plastic strain increment occurs.

Note that similar stress-dilatancy relationships were mentioned in Muhunthan and Sasiharan [34].

(16) Tasiopoulou and Gerolymos [55]:
Tasiopoulou and Gerolymos [55] presented their stress-dilatancy equation as follows:

$$d = M_{PT} - \zeta M_s$$  \hspace{1cm} (45)$$

where $M_{PT}$ is the phase transformation stress ratio, $M_s$ is ultimate strength stress ratio in $q-p'$ space, and $\zeta$ is the hardening parameter which evolves with shearing and is defined as:

$$\zeta = \left|\frac{q}{M_s p}\right|^n$$  \hspace{1cm} (46)$$

where $n$ is an exponential parameter which controls the distance of the current stress state from the failure line.

The $\zeta$ parameter is bounded. Its values limit within the range of $[-1, 1]$.

(17) Kan et al. [21]:
Kan et al. [21] used the following plastic potential function:
\[
\begin{align*}
\left\{ \begin{array}{ll}
g(p,q,\theta,p_0) = \tilde{\tau}q + \frac{AM(\theta)p}{A-1}\left(\frac{p}{p_0}\right)^{\frac{1}{A-1}} & \text{for } A \neq 1 \\
g(p,q,\theta,p_0) = \tilde{\tau}q + M(\theta)p \ln\left(\frac{p}{p_0}\right) & \text{for } A = 1
\end{array} \right.
\end{align*}
\]
(47)

in which \(p_0\) controls the size of the plastic potential surface, and \(A\) is a material parameter.

\(\tilde{\tau}\) is a scalar whose sign controls the direction of plastic flow. It takes value of 1 or -1 depends on relative positions of the stress point, \(\sigma'\), on the yield surface and its corresponding image point, \(\sigma\), on the bounding surface.

\(M(\theta)\) is calculated as a function of load angle, \(\tilde{\theta}\), as follows:

\[
M(\tilde{\theta}) = M\left(\frac{2\alpha^4}{1 + \alpha^4 - (1 - \alpha^4) \sin 3\tilde{\theta}}\right)^{\frac{1}{3}}
\]
(48)

Where load angle \(\tilde{\theta}\) is defined as:

\[
\tilde{\theta} = \frac{1}{3} \sin^{-1}\left(-\frac{3\sqrt{3}}{2} \frac{f_3}{\sqrt{J_2^3}}\right)
\]
(49)

in which \(J_2\) and \(J_3\) are the second and third invariants of the deviatoric stress tensor. Note that the load angle ranges from \(\tilde{\theta} = 30\) for triaxial compression to \(\tilde{\theta} = -30\) for triaxial extension.

\(\alpha\) is determined by below relation:

\[
\alpha = \frac{3 - \sin \varphi_{cs}}{3 + \sin \varphi_{cs}}
\]
(50)

\(M\) is the value of the critical state stress ratio under triaxial compression which is linked to the critical state friction angle as:

\[
M = \frac{6\sin \varphi_{cs}}{3 - \varphi_{cs}}
\]
(51)

The direction of plastic flow in this model is calculated based on the following relations:

\[
m_g = \frac{\partial g}{\partial \sigma} \left[ \frac{\partial g}{\partial \sigma'} \right]^{-1}
\]
(52)

\[
\partial g/\partial \sigma'\text{ is evaluated by applying the chain rule of differentiation as follows:}
\]

\[d = d_1 \left[ 1 + \frac{R}{M(\theta)} \right] \left[ M(\theta) \exp(m_1\zeta_{g} - R) - 1 \right]
\]
(54)

where \(d_1\) and \(m_1\) are two model constants. \(\zeta_{g}\) is defined as follows:

\[
\zeta_{g} = \xi - e_A(A - 1)
\]

where \(e_s\) is a model parameter, \(\xi = e - e_{cr}\) is the state parameter, \(A\) is a fabric anisotropy variable, \(R\) is the stress ratio tensor which is defined as:

\[
R = \frac{S_i}{\sigma_{ij}}\delta_{ij}
\]

in which \(\sigma_{ij}\) is the stress tensor, \(p = \sigma_{ij}/3\) is the mean normal stress, \(\delta_{ij}\) is the Kronecker delta and \(S_{ij}\) is the deviator stress. \(g(\theta)\) is defined based on the load angle \(\theta\) as:

\[
g(\theta) = \frac{\sqrt{(1 + c^2)^2 + 4c(1 - c^2)\sin 3\theta} - (1 + c^2)}{2(1 - c)\sin 3\theta}
\]
(55)

where \(c = M_e/M_c\) is the ratio between the critical state stress ratio in triaxial extension \(M_e\) and that in triaxial compression \(M_c\).

\(A\) is defined based on product of the fabric tensor \(F_{ij}\) and the loading direction tensor \(n_{ij}\) as:

\[
A = F_{ij}n_{ij}
\]
(56)

where \(F_{ij}\) is a symmetric tensor whose norm \(F = \sqrt{F_{ij}F_{ij}}\) is named as the degree of fabric.

(19) Qu and Huang [39].

Similar to Li and Dafalias [29], dilatancy of sand was related to state parameter \(\xi\) and the current stress ratio \(\eta = q/p\) by Qu and Huang [39] as follows:

\[
d = \frac{d_0}{M} [M(\theta) e^{mt} - \eta]
\]
(57)

where \(d_0\) and \(m\) are material parameters and \(M\) is the critical state stress ratio under triaxial compression.

\(g(\theta)\) is defined similar to the definition which was given in Gao et al. [11]. \(\theta\) is the load angle which is defined similar to Kan et al. [21].

Mean effective stress \(p'\) and deviatoric stress \(q\) are calculated by \(p' = I_1/3\) and \(q = \sqrt{3}I_2\) in which \(I_1\) is the first invariant of the effective stress tensor and \(J_2\) is the second invariant of the deviatoric stress tensor.

The proposed stress-dilatancy relationship gives rise to the following plastic potential function:
Jin et al. [20] presented the following stress-dilatancy equation for cohesionless sands:

\[ d = d_0 (M_{PT} - \eta) \exp \left[ h_2 \left( \frac{e}{e_{cr}} - 1 \right) \right] \]  

(59)

where \( h_2 \) is a material parameter and \( d_0 \) is a positive constant which controls the magnitude and evolution of dilatancy rate.

\( M_{PT} \) is the current phase transformation stress ratio, \( \eta \) is the current stress ratio, \( e \) is the current void ratio, and \( e_{cr} \) is the critical state void ratio.

The term \( \left( e/e_{cr} - 1 \right) \) is used to adjust dilation or contraction of loose and dense sands. For loose sands \( e > e_{cr} \) and \( \eta < M_{PT} \), now if \( h_2 > 0 \) then the exponential term increases the rate of contraction as \( d_0 \) does. Also if \( h_2 < 0 \) then the exponential term decreases the rate of contraction. However as shearing continues towards the critical state, the effect of the exponential term on the stress dilatancy diminishes because the exponential term approaches zero.

When stress state reaches the critical state, the exponential term totally disappears and \( M_{PT} = \eta \) which guarantees zero dilatancy rate at the critical state.

Sun et al. [53] investigated the effect of particle breakage on the stress-dilatancy behavior of granular soils and proposed the following plastic flow rule with modification of Rowe’s equation:

\[ d = \frac{9(M - \eta) + 9\eta \chi}{9 + 3M - 2M\eta - \chi} \]  

(60)

where

\[ \chi = \frac{\gamma (6 + 4M) (3 - M)}{3 (6 + M)} \]  

(61)

in which \( \gamma \) is a material parameter which slightly depends on confining pressure. \( M \) is the critical state stress ration under triaxial compression. Therefore, \( x \) is a constant.

Yin et al. [70] suggested the following simple non-associated plastic potential function:

\[ g(p', q) = \frac{q}{M_{PT}} p + \ln \left( \frac{p'}{p_c} \right) \]  

(62)

where \( M_{PT} = 6 \sin \varphi_{PT} / (3 - \sin \varphi_{PT}) \) in which \( \varphi_{PT} \) is the phase transformation or characteristic angle which corresponds to transition from the contractive to dilative behavior.

Sun and Xiao [52] presented the following plastic potential function for granular soils:

\[ g = (2p' - p'_o)^2 + \left( \frac{2q}{M} \right)^2 - p'_o^2 \]  

(63)

where \( p'_0 \) controls the size of the plastic potential surface, \( p' \) is the mean effective stress, and \( q \) is the deviatoric stress.

When the sand is sheared from a dense state where the state parameter is negative (\( \xi < 0 \)), \( \alpha_d \) would increase with shearing until the critical state is ultimately reached when \( \xi = 0 \), \( \alpha_d = 1 \) and \( d = 0 \). However, if the sand is initially at a loose state where the state parameter is positive (\( \xi > 0 \)), \( \alpha_d \) would decrease until the critical state is reached when \( \xi = 0 \), \( \alpha_d = 1 \), and \( d = 0 \).

### 3.2 Cemented Sands

A summary of the following stress-dilatancy relationships and plastic potential functions of cohesive sands with important highlights is given in table 4 (see appendix section).

Vermeer and De Borst [59] presented Rowe’s stress-dilatancy equation in terms of mobilized dilation and friction angle takes the following form:

\[ \sin \psi_m = \frac{\sin \varphi_m - \sin \varphi_{cr}}{1 - \sin \varphi_m \sin \varphi_{cr}} \]  

(66)

where \( \varphi_{cr} \) is the constant volume or critical state friction angle. \( \varphi_m \) is the mobilized dilatancy angle which is a function of plastic strain as the mobilized friction angle (\( \varphi_m \)) does. Thus, change in \( \psi_m \) can be predicted by change in \( \varphi_m \).

The above equation was initially proposed by Vermeer and De Borst [59] for soils, rocks and concrete. However,
this form of Rowe’s equation can not describe the density or void ratio dependency during shearing. In order to address this shortcoming, a modification of the original Rowe’s equation was proposed by Wan and Guo \cite{60} as follows:

\[
\sin \psi_m = \frac{\sin \varphi_m - \left( e / e_c \right)^{0.44} \sin \varphi_{cr}}{1 - \left( e / e_c \right)^{0.44} \sin \varphi_m \sin \varphi_{cr}}
\]  

(67)

where \( e \) is the current void ratio, \( e_c \) is the critical state void ratio, and \( \omega_d \) is a material parameter. Parameter \( \omega_d \) can also be linked to fabric tensor, plastic shear strain and the effect of intermediate principal stress measured by parameter \( b = (\sigma_2 - \sigma_3) / (\sigma_1 - \sigma_3) \).\cite{60}.

(2) Kim and Lade \cite{24}:

Based on variety of experimental observations, Kim and Lade \cite{24} suggested the following equation for the plastic potential function of cohesive and non-cohesive frictional materials:

\[
g(I_1, I_2, I_3) = \left( \psi_1 I_1^2 + \psi_2 I_2 + \psi_3 \right)^\mu
\]  

(68)

where \( \psi_1, \psi_2, \) and \( \mu \) are the plastic potential parameters, \( p_a \) is the atmospheric pressure and \( I_1, I_2, \) and \( I_3 \) are the first, second, and third invariant of the stress tensor which are defined based on the three principal stresses (observed during triaxial tests) as follows\cite{24}:

\[
I_1 = \sigma_1 + \sigma_2 + \sigma_3
\]  

(69)

\[
I_2 = - (\sigma_1 \sigma_2 + \sigma_2 \sigma_3 + \sigma_3 \sigma_1)
\]  

(70)

\[
I_3 = \sigma_1 \sigma_2 \sigma_3
\]  

(71)

Reddy and Saxena \cite{45}, Lade and Kim \cite{26}, Kandasami et al. \cite{22}, Singh et al. \cite{50}, and Singh et al. \cite{51} used the above plastic potential function in their constitutive model to simulate the plastic flow of cemented and uncemented geomaterials.

(3) Van den Hoek and Geilikman \cite{58}:

Van den Hoek and Geilikman \cite{58} presented the following plastic potential function for sandstone in analysis of sand production in petroleum wells:

\[
g = \frac{1}{2} (\sigma'_\omega - \sigma'_r) - \frac{1}{2} (\sigma'_\omega + \sigma'_r) \sin \psi + \text{constant}
\]  

(72)

where \( \psi \) is the dilation angle, \( \sigma'_\omega \) is the tangential effective stress and \( \sigma'_r \) is the radial effective stress. Constant value has no impact on the model since only the derivative of the plastic potential function is influential in constitutive model.

(4) Arroyo et al. \cite{3}:

Arroyo et al. \cite{3} proposed the following stress-dilatancy equation for cemented sands:

\[
d = m_g (M - \eta) \left( \frac{a_g M}{\eta} \right)
\]  

(73)

where \( m_g, a_g, \) and \( M \) are model parameters which control the shape of the plastic potential surface.

Note that the above stress-dilatancy relationship is similar to that presented by Lagioia et al. \cite{27}, Buscarnera and Laverack \cite{9} also used the similar flow rule as above in their constitutive model presented for porous rocks.

(5) Yu et al. \cite{73}:

The following stress-dilatancy relationship was proposed by Yu et al. \cite{73} for cemented soils:

\[
d = \frac{9(M - \eta) + 6 \frac{\text{coh}}{p} \sqrt{(2M + 3)(-M + 3)}}{9 + 3M - 2M \eta + 4 \frac{\text{coh}}{p} \sqrt{(2M + 3)(-M + 3)}}
\]  

(74)

where \( \text{coh} \) is the interparticle cohesion. Original Rowe’s flow rule can be recovered by setting \( \text{coh} = 0 \). In this model, cohesion was assumed to degrade with the total plastic strain increment as follows:

\[
d \text{coh} = \text{coh} \exp \left( -\sigma_{\text{d}} \cdot \sqrt{(\dot{e}_q^P)^2 + (\dot{e}_p^P)^2} \right)
\]  

(75)

where \( \sigma_{\text{d}} \) determines rate of cohesion degradation.

The plastic potential function corresponds to the above stress-dilatancy equation is as follows\cite{73}:

\[
g = 3M \ln \left( \frac{p'_r + p'_t - k_g}{\sigma_y} + (2M + 3) \ln \frac{2(q - h_g)}{p'_r + p'_t - k_g} + 3 \right) + (M - 3) \ln \left( 3 - \frac{q - h_g}{p'_r + p'_t - k_g} \right)
\]  

(76)

\[
k_g = \sqrt{(3 + 2M)(3 - M)(36 - 12M)\text{coh}}
\]  

(77)

\[
h_g = \sqrt{(3 + 2M)(3 - M)(-54 + 18M)\text{coh}}
\]  

(78)

Rahimi et al. \cite{41}, Rahimi et al. \cite{42} and Rahimi et al. \cite{44} used the same stress-dilatancy relationship as that proposed by Yu et al. \cite{73} by replacement of constant critical state stress ratio with variable phase transformation stress.
ratio.

(6) Wang and Leung \[63\].

Wang and Leung \[63\] presented the following stress-dilatancy relationship for cemented sands in triaxial condition (i.e. an axisymmetric condition):

\[
q \dot{e}_q^p + p \dot{e}_p^p = M p \dot{e}_q^p + \Delta W_{bond} \tag{79}
\]

or

\[
\frac{q}{p} + \frac{\dot{e}_p^p}{\dot{e}_q^p} = M + \frac{\Delta W_{bond}}{p \dot{e}_q^p} \quad \text{or} \quad d = M - \eta + \frac{\Delta W_{bond}}{p \dot{e}_q^p} \tag{80}
\]

where \(\Delta W_{bond}\) is the total energy which is dissipated due to breakage or destruction of the cementing bond.

Ajourloo et al. \[1\] also suggested the same stress-dilatancy relation for cemented sands. However, neither Wang and Leung \[63\] nor Ajourloo et al. \[1\] did not put forward any formulas for \(\Delta W_{bond}\). Suggestion of any relationship for \(\Delta W_{bond}\) will be considered as a contribution for the stress-dilatancy relation of cemented sands.

(7) Zhang and Salgado \[74\].

Since original Rowe’s stress-dilatancy relationship does not produce correct volumetric response for cemented materials \[73, 74, 40, 41\], a modification of Rowe’s equation was proposed by Zhang and Salgado \[74\] as follows to address this deficiency:

\[
\frac{\sigma_1}{\sigma_3} = K \left( 1 - \frac{\dot{\varepsilon}_v}{\dot{\varepsilon}_1} \right) + \frac{2 \text{coh}}{\sigma_3} K \sqrt{1 - \frac{\dot{\varepsilon}_v}{\dot{\varepsilon}_1}} \tag{81}
\]

where \(K\) is a parameter which depends on the failure friction angle, \(\sigma_1\) and \(\sigma_3\) are the major and minor principal effective stresses, respectively, \(\dot{\varepsilon}_v\) and \(\dot{\varepsilon}_1\) are the volumetric and major principal strain increment.

The above equation can be written in terms of the mean effective stress \(p\), the deviator stress \(q\), and the critical state stress ratio under compression \(M\) as follows:

\[
d = \frac{9(M - \eta) - 3m_c}{9 + 3M - 2\eta M + m_c} \tag{82}
\]

where \(m_c\) is related to the cohesion as follows:

\[
m_c = \frac{6(-M + 3\text{cof} + \sqrt{p})}{-\eta + 3} = \frac{2\text{cof}(-M + 3)}{\sqrt{-\eta + 3}} \tag{83}
\]

Where \(\text{cof}\) is the interparticle cohesion.

Note that Zhang and Salgado \[74\] and Yu et al. \[72, 73\] stress-dilatancy relationships have been mentioned in Porcino and Marciano \[38\] as well.

(8) Gao and Zhao \[10\]:

Gao and Zhao \[10\] presented the following flow rule for cemented sands:

\[
d = \frac{d_1}{\exp\left(\int \left(\frac{dL}{dF}\right)\right)} (M_{PT} d_C d_F - H) \tag{84}
\]

where \(d_1\) is a positive model parameter, \(M_{PT}\) is the phase transformation stress ratio, \(H\) is hardening parameter, \(DL\) is a loading index and \(\int \left(\frac{dL}{dF}\right)\) denotes the Macauley bracket with \(\int \left(\frac{dL}{dF}\right) = 0\) when \(x \leq 0\) and \(\int \left(\frac{dL}{dF}\right) = x\) when \(x > 0\). The role of the denominator in above equation is to control the volume change, especially when the strain level is high. As the sample is sheared to the critical state, the increment of the plastic deviatoric strain is unlimited. At this state, the denominator term would reach infinity making the value of the dilatancy rate \(d\) zero. The two parameters \(d_C\) and \(d_F\) are used to characterize the bonding and anisotropic effects, respectively, as follows:

\[
d_C = \exp\left( -c_0 \sqrt{\frac{\sigma_0}{p_T}} \right) \tag{85}
\]

\[
d_F = \exp(k(A + 1)) \tag{86}
\]

where \(C_0\) and \(k\) are positive model constants, \(\sigma_0\) denotes the current triaxial tensile strength of the material, \(p_T\) is a reference pressure and \(A\) is an anisotropic variable dependent on fabric tensor whose definition has given in Gao and Zhao \[10\].

Above equations imply that as the value of tensile strength increases, \(d_C\) decreases which leads to a reduction in value of the dilatancy rate \(d\). The material response is less contractive and hence the liquefaction resistant increases. Also \(d_F\) increases with \(A\) (the major principal stress direction becomes closer to the direction of deposition) which in turn results in larger value of the dilatancy rate \(d\) and hence more contractive response and less resistant to the liquefaction \[10\].

(9) Weng \[65\]:

In his generalized plasticity model for sandstone, Weng \[65\] used Nova and Wood \[36\] stress-dilatancy relationship which has been proposed for cohesionless sands. This, however, is a questionable choice because cemented sands show more dilatave behavior than un cemented sands \[40, 41\]. This can not be reproduced simply by using the flow rule developed for cohesionless sands.

(10) Rios et al. \[46\]:

Rios et al. \[46\] applied Rowe’s stress-dilatancy relation (equation 10) in their constitutive model developed for modelling bonded soils. This is controversial. As men-
tioned already, the stress-dilatancy relationships proposed for cohesionless sands do not work for cemented or bonded sands because volumetric behavior of uncemented sands is different than that of cemented sands [40, 41].

4. Conclusion
Some important stress-dilatancy relationships and plastic potential functions proposed for uncemented and cemented sands were reviewed in this article. The paper suggests that unlike uncemented sands for which intensive research has been performed by different researchers, there are a few researches on the stress-dilatancy relationships of cemented sands. To fill this gap, considerable effort is needed. Therefore, it is recommended that this area of cemented sands is chosen as a potential research title for future studies. Modification of Rowe’s equation can be a step forward to account for deficiencies of the previous stress-dilatancy relationships proposed for cemented sands.

Conflicts of interest
The corresponding author confirms that there is no conflict of interest.

Appendix
Summary of aforementioned flow rule and plastic potential equations for uncemented and cemented sands

Table 3. Summary of proposed stress-dilatancy and plastic potential relationships for uncemented sands

<table>
<thead>
<tr>
<th>Proposed stress-dilatancy relationship or plastic potential function</th>
<th>Methodology/Application/Validation (Calibration)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nova and Wood [16]</td>
<td>-proposed on the basis of experimental works on sand in plane strain &amp; triaxial conditions. -when μ=1, the equation reduces to that of the Cam Clay model. -verified against constant p and constant q laboratory tests with great matches.</td>
</tr>
<tr>
<td>Nova and Wood [16]</td>
<td>-One of the oldest and most popular stress-dilatancy relationships. -This relationship has been employed by many researchers like Pastor et al. [35], Haeri and Hamidi [36], Hamidi and Yarbakhti [41] and Kong et al.</td>
</tr>
<tr>
<td>Jefferies [17]</td>
<td>-proposed in his critical state constitutive model. -when N=0, the equation reduces to the familiar Cam Clay model. -the influence of void ratio and mean effective stress on sand response is captured well but the influence of fabric is neglected.</td>
</tr>
<tr>
<td>Lagoia et al.[35]</td>
<td>-proposed such that it predicts zero dilatancy rate in the critical state and infinite dilatancy rate in zero stress ratio. -verified against drained triaxial tests with excellent matches.</td>
</tr>
</tbody>
</table>

Yu [30] -proposed for both sand & clay based on Rowe’s stress-dilatancy relationship. -verified against drained & undrained triaxial compression tests of sand & clay with very good agreements.

Schanz et al. [11] -proposed based on concept of mobilized dilatancy angle, mobilized friction angle and critical state friction angle. -the mobilized friction angle is estimated by shape of a Mohr-Coulomb failure envelope. -calibrated for drained & undrained behavior of Hostun loose sand under oedometer & triaxial tests.


McDowell [10] -the flow rule is non-associated. Hence, the critical state point does not happen at the top of yield surface. -fulfills the necessary conditions of zero shear strain under isotropic conditions and infinite shear strain with zero volumetric strain at the critical state. This approach is identical to that suggested by Lagioia et al. [27]. -performance of the model was discussed, however, it was not verified against experimental observations.

Russell and Khalili [16] -A state parameter dependent stress-dilatancy equation within critical state framework. -Comparison of predicted volumetric behavior with experimental results (under isotropic & oedometer compression, and drained & undrained triaxial tests) suggests a great credit for the proposed equation.

Dafalias and Manzari [14] -a fabric dependent stress-dilatancy equation based on difference between the current stress ratio and the phase transformation stress ratio. -The model predicts a phase transformation stress ratio equal to the current stress ratio at the critical state which results in zero dilatancy rate (permanent steady state response). -calibrated against drained & undrained monotonic & cyclic compression tests. Predicted volumetric responses were in very good harmony with experimentally measured behaviors.

Khalili et al. [10] -similar to equation of Russell and Khalili [20]. -verified excellently against drained & undrained triaxial compression & extension tests of sand & clay with very good agreements.

Imam et al. [14] -similar to equation of Dafalias and Manzari [26]. -however, it is not fabric dependent. -proposed for both triaxial compression and triaxial extension. -volumetric response was validated against many drained & undrained triaxial compression & extension tests on Ottawa and Toyoura sands under monotonic loading with appreciable matches.

Ling and Yang [26] -a combination of relationships proposed by Nova and Wood [16] and Li and Dafalias [29]. -a variable stress ratio (M) is used in this equation rather than the constant critical state stress ratio (M). -wonderful performance of the equation was proved by calibration of drained & undrained volumetric behavior of Toyoura & Nevada & Fuji River sands under monotonic & cyclic loading.
Table 4. Summary of proposed stress-dilatancy and plastic potential relationships for cemented sands

<table>
<thead>
<tr>
<th>Proposed stress-dilatancy or plastic potential function</th>
<th>Methodology/Application/Validation (Calibration)</th>
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<tr>
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<td>-Similar to Jeffries’s approach, Sasiharan con-</td>
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<td>tion, obtained by integration of the flow rule,</td>
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<td>identical to the yield function.</td>
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<td>-calibrated against drained &amp; undrained triaxial</td>
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<td>compression tests under monotonic &amp; cyclic</td>
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<td>loading with good matches.</td>
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<tr>
<td>Tasiopoulou and Gerolymos [46]</td>
<td>-a hardening parameter &amp; phase transformation</td>
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<td>stress ratio dependent equation.</td>
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<td>-performance of the model was examined but it</td>
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<td>was not validated against experimental observa-</td>
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<td>Kan et al. [51]</td>
<td>-a relatively complex equation for plastic poten-</td>
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<td>tial function.</td>
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<td>-calibrated successfully against drained &amp;</td>
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<td>undrained cyclic tests on loose &amp; dense samples</td>
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<td>of Toyoura &amp; Fuji River sands.</td>
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<td>Gao et al. [50]</td>
<td>-a relatively complex fabric-dependent dilatancy</td>
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<td>of Toyoura &amp; Fraser River sands under different</td>
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<td>loading conditions.</td>
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<td>Qu and Huang [59]</td>
<td>-a state parameter dependent dilatancy equation.</td>
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<td>-was not verified based on experimental obser-</td>
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<td>vations.</td>
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<td>Jin et al. [52]</td>
<td>-a void ratio &amp; phase transformation stress ratio</td>
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<td>dependent equation.</td>
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<td>-calibrated based on drained &amp; undrained triaxial</td>
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<td>compression tests of Nevada &amp; Toyoura sands under</td>
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<td>monotonic &amp; cyclic loading.</td>
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<tr>
<td>Sun et al. [53]</td>
<td>-a modified version of Rowe’s equation which</td>
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<td>considers the effect of particle breakage.</td>
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<td>-was calibrated against plastic flow of Yixing</td>
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<td>rockfill, Kish Island &amp; Cambria sands.</td>
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<td>Yin et al. [59]</td>
<td>-a simple non-associated plastic potential func-</td>
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<td>tion suggested for very coarse granular materi-</td>
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<td>-calibrated based on drained triaxial tests on</td>
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<td>rockfill materials with different grain sizes.</td>
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<td>Sun and Xiao [54]</td>
<td>-a state parameter dependent dilatancy equation</td>
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<td>for granular soils subjected to monotonic triaxial</td>
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<td>-calibrated successfully against drained &amp;</td>
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<td>undrained triaxial compression tests on various</td>
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<td>granular soils.</td>
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ARTICLE

Living Matter and the Laws of Thermodynamics for the Biosphere

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ABSTRACT

The laws of thermodynamics have been developed for inert matter, and living matter has not been considered as a variable in these laws. Living matter possesses properties that have had major effects on biosphere evolution with time. The zeroth property is “Living matter is produced from living matter only.” The first property may be summarized as “Living matter occupies the available spaces to the maximum extent when environmental conditions are favorable and no obstacles are present.” And the second property is “Living matter mutates, changes, and adapts to maintain the continuity of life and size as large as possible when environmental conditions are unfavorable.” While the zeroth property is objective in nature, the first and second properties are subjective, in that they are driven by internal stimuli characterizing living matter. Their interaction with the laws of thermodynamics may be thought of as “philosophy intertwining with science.” Accordingly, the laws of thermodynamics are revised to factor in life as a variable. Mathematical expressions of the first and second laws are derived and some of their applicability to the biosphere and climate is explained and discussed. The main conclusion is that life changes climates and the fabric of the biosphere.

1. Introduction

Planetary motion is characterized by conservation of the angular momentum and infinitesimal variation of orbital eccentricity. These characteristics yield a constant annual solar energy exchanged with any planet, regardless of orbit shape. A planet thus reaches thermodynamic equilibrium. Seasonal or orbital variations induce thermodynamic transformations displaced differentially from equilibrium. They are, therefore, reversible based on the laws of thermodynamics, and lifeless planets may not have relevant directional thermodynamic transformations.

This is not what is observed on planet earth. The geological record is rich with data revealing steady evolution of living matter, surface geology, and climate. Clearly, life on earth has made a difference, and the first and second laws of thermodynamics must be revised for the biosphere. This sphere includes living and inert matters that interact with each other, and this interaction was not accounted for in the original formulation of the laws of thermodynamics. They were developed for practical applications, where systems’ surroundings are part of the biosphere such as land, air, and water. The entire system and its surroundings were made of inert matter. Conversely, biosphere thermodynamic transformations are interactions between living and inert matters, and they changed climates of the past as well as present-day climates.

The biosphere as a thermodynamic system where living and inert matters interact comprises land, surface water,
living matter in the sea and on the land, and atmospheric air. These biosphere subsystems observe biological, chemical, and thermodynamic changes with variation in the size of life. Because the size of the non-green living matter depends on the size of the green matter, variation in the size of life is equal to variation in the chemical energy of photosynthesis. An increase in the size of photosynthesis converts more solar energy into chemical energy in plant tissues and the surroundings receive less solar energy and vice versa. Consequently, photosynthesis exchanges heat that is in transit in the biosphere and may be treated as such. Therefore, the first property of living matter intertwines with the first law of thermodynamics. So does the second property: Unlike lifeless planets, biosphere thermodynamic transformations have a steady direction, irreversible, and the second law of thermodynamics must be revised as well.

In this work, the interactions of the basic properties of living matter and the laws of thermodynamics are discussed, derivation of the revised laws of thermodynamics to account for life in the biosphere is provided, and the significance of the derived laws is explained.

2. Background Information

The zeroth and first properties of living matter were proposed and thoroughly discussed by [1]. There is overwhelming evidence of their validity. Not a single living cell that eats, secretes, and multiplies has been produced in laboratory experiments. Nor is there evidence of living cells being a product of purely inert matter. Such overwhelming evidence is a reasonable basis to claim that “Living matter is produced from living matter only.” Similarly, our basic observations indicate that living matter has an inherent and intrinsic nature to multiply and increase in number when the conditions are favorable and no obstacles are present. This is true for single living cells as well as complex organisms, and there is overwhelming proof of the validity of this conclusion as well.

The innate nature of living matter to adapt, change, and mutate when environmental conditions are unfavorable or vary is observed throughout the geological record. Bacteria mutation in response to medicine and subsequent resistance maintains the continuity of life and bacteria count to the maximum extent. Also, this is true for plants, insects, animals, and humans. Plants adapt, change, produce venoms, lignin, and rise above the ground to occupy the available spaces as much as practically possible. Variation in climates with latitude has produced fauna and flora characteristic of each latitude. Plants shed their leaves in cold climates to maintain the continuity of their existence. The evidence that “Living matter mutates, changes, and adapt to maintain the continuity of life and size as large as possible when environmental conditions are unfavorable” is overwhelming as well. These inherent natural properties of living matter exchange energy that interacts with the thermodynamics of the biosphere. Therefore, they must be accounted for in the laws of thermodynamics.

Thermodynamics is an established branch of science that addresses transformations where heat and work are exchanged between thermodynamic systems and their surroundings. Reference [2] presents the current understanding of thermodynamics applicable to systems involving inert matter only. “Postulate 1: There exists a form of energy known as internal energy $U$, which for systems in equilibrium states is an intrinsic property of the system, functionally related to the measurable coordinates which characterize the system. Postulate 2: the total energy of any system and its surroundings is conserved. (First law of thermodynamics).” Mathematically, this law may be written as follows:

\[ dU = dQ - dW \quad (1) \]

Where $Q$ is heat crossing the boundary of the thermodynamic system. The convention is to consider the heat as positive if added to the thermodynamic system. The symbol, $W$, denotes the work exchanged between system and surroundings, considered together, resulting from any real process that approaches reversibility.

“Postulate 3: There exists a property called entropy $S$, which for systems in equilibrium states is an intrinsic property of the system, functionally related to the measurable coordinates which characterize the system. For reversible processes changes in this property may be calculated by the equation

\[ dS = \frac{dQ_{rev}}{T} \quad (2) \]

Where $T$ is the absolute temperature of the system and $Q_{rev}$ is the reversible heat.

Postulate 4: The entropy change of any system and its surroundings, considered together, resulting from any real process is positive and approaches a limiting value of zero for any process that approaches reversibility. (Second law of thermodynamics).”

Equations (1) and (2) apply for closed thermodynamic systems where the system and surroundings exchange energy only and matter is not exchanged. The mass of system or surroundings remain constant. If the system in thermodynamic equilibrium gains heat, it undergoes a spontaneous thermodynamic transformation until a new equilibrium is reached. In the process, heat and work are
exchanged between system and surroundings. Thermodynamic characteristics such as system pressure, temperature, and concentrations may be used as coordinates to define states of thermodynamic equilibrium. A thermodynamic transformation differentially displaced from equilibrium may be considered as a reversible transformation, in that the system may spontaneously return to its original characteristic coordinates when the cause of displacement ceases.

The biosphere as defined in the introduction section has a constant mass and exchanges energy with its surroundings. Therefore, it may be considered as a closed thermodynamic system and the first and second laws of thermodynamics thus apply. However, living matter is not considered in these thermodynamic relationships. The size of green matter is a coordinate of the biosphere thermodynamic system, and the energy exchanged resulting from the variation in its size is heat in transit that must be accounted for. Therefore, for the biosphere the first and second laws of thermodynamics should be revised to account for life in the biosphere. The subject is important because variation in the size of photosynthesis varies the heat content of the biosphere and changes climates. Similarly, deforestation is a reversed process of photosynthesis and it produces heat in the climate. Therefore, deriving the first and second laws of thermodynamics for the biosphere is important for research and society.

3. Revising the First and Second Laws of ThermoDynamics for the Biosphere

Publications \(^{[3,4]}\) discuss the present state of photosynthesis understanding. It is a chemical reaction where water and carbon dioxide are converted into sugars, cellulose, carbohydrates and other plant constituents. Solar radiation and chlorophyll are required for the chemical reaction; it is an endothermic and non-spontaneous reaction. The solar energy is ultimately converted into chemical energy stored in plants’ tissues, and biosphere subsystems loose this energy. While an increase in the size of photosynthesis removes heat from the biosphere, deforestation, decay, or combustion of green matter add heat to the biosphere because it is the reversed process of photosynthesis. If the chemical energy of green matter is indicated by \(Q_g\), the first law of thermodynamics may be revised for the biosphere

\[
dU = dQ_g + dW
\]

Where \(U\) is now equal to the internal energy of the biosphere and \(W\) is the work exchanged in the biosphere. Not considered in this last equation radiative terms of biosphere subsystems. The reason is that life-dependent thermodynamic transformations are states differentially displaced from each other and the original starting thermodynamic state. Should this state be assumed to be in thermodynamic equilibrium, which is a reasonable assumption, radiative terms cancel out and may be eliminated from the equation. The same is true for all other thermodynamic states differentially displaced from the state of equilibrium.

The main biosphere subsystems are surface and atmosphere. Therefore

\[
dU_s + dU_a = dQ_g + dW_a
\]

Where the subscript “s” denotes surface and “a” for atmosphere. Because atmospheric air is surrounded by outer space whose pressure is negligible, variation in the internal energy of the atmosphere, \(dU_a\), is equal to variation in its enthalpy, \(dH_a\). The internal energy of the surface is equal to the heat of the surface \(Q_s\). The work, \(W_a\), is mainly potential energy of the atmosphere. Therefore, the first law simplifies.

\[
dQ_g = dQ_s = (dW_a + dH_a)
\]

The term \((dW_a + dH_a)\) is energy exchanged between atmosphere and surface. It is equal to the opposite sign of the heat of carbon conversion to carbon dioxide, \(dQ_c\), based on \(^{[5]}\). Consequently

\[
dQ_c = dQ_g + dQ_s \quad (1-r)
\]

The sum of surface heat and chemical energy of the biosphere is conserved.

Not mentioned in this form of the first law for the biosphere is the word surroundings. The reason is that the surroundings of the biosphere as defined in the introduction section are outer space and solid earth underneath the biosphere. Outer space is empty and no chemical energy, potential energy, or heat may be exchanged with outer space. The same is true for the solid earth; it is thick and rigid and the amount of energy exchanged with the solid earth may be neglected. The sign of \(dQ_s\) is negative if the size of the green matter increases and positive if the size decreases. Also, variation in the heat of carbon conversion \(dQ_c\) changes sign. It is positive when the content of carbon dioxide in the atmosphere increases and negative if the content decreases.

It should be noted that the chemical energy defined in this work is the energy associated with thermodynamic processes that exchange carbon in the biosphere. This energy interacts with the laws of thermodynamics according to Equation (1-r). Carbon free processes do not produce
energy interaction and must exit the biosphere and climate system. Examples of these processes include but not limited to generation of earth’s internal heat, transmission of energy of geological activities, and production of carbon-neutral energy.

On the other hand, the thermodynamic transformations caused by life are small displacements from each other. For instance, the present warming trend is less than one degree Kelvin in approximately 250 years. If compared with biosphere temperature of 288 K, the current climate change is in fact an incremental displacement from equilibrium. On an annual basis, biosphere transformations are infinitesimal processes. The same is true for all of past changes in climate. Even though they are infinitesimal displacements from equilibrium, they may not be assumed to be reversible, in that life adapts, evolves, and resists death and annihilation when environmental conditions are unfavorable. As a result, the second law of thermodynamics for the biosphere may be written as follows:

\[ \text{d}S > 0 \quad \text{(2-r)} \]

The entropy of the biosphere increases with time.

Here, too, the word surroundings is removed for the same reasons discussed earlier. Equation (2-r) reveals that biosphere thermodynamic transformations are irreversible.

4. Discussion and Conclusions

The zeroth property of the living matter announces the resilience and strength of living matter as a continuous and unbreakable chain extending throughout eons. Living matter is indestructible; however, it may mutate or assume different shapes or forms. The first property on the other hand states that the size of life can never reach a steady value, it is inherently variable. As a result, the energy produced by life is energy transient in the biosphere that exchanges heat and work, Equation (1-r). The biosphere can never reach a thermodynamic equilibrium that characterizes thermodynamic systems of inert matter alone. Thermodynamic transformations driven by life in the biosphere are infinitesimal displacements around equilibrium. Yet, they are irreversible as the revised second law of thermodynamics for the biosphere reveals, Equation (2-r). This fundamental difference between thermodynamic systems where life is a variable and thermodynamic systems made of inert matter is of paramount importance. All life driven thermodynamic transformations have a direction. They are irreversible, and steady evolution of the biosphere is a natural outcome as a result that cannot come to a halt.

These thermodynamic conclusions for the biosphere are in agreement with the geological record. Life and biosphere has had a steady and uninterrupted evolution throughout geological time. The geological record is rich with overwhelming fossil samples supporting simultaneous evolution of life and biosphere. The age of surface rocks are predominately much younger than the age of the earth, and younger rocks are in the making at the present time. Living matter produced these younger rocks through biosynthesis of calcite, phosphate, and the large number of minerals that can be obtained from them such as chalk, gypsum, dolomite, fossil fuels, and others. Life has produced beautiful surface landscapes and majestic mountains made of sedimentary rocks around the world, thus testifying to the continuity, resilience, and power of living matter.

As Equation (1-r) reveals, variation in the size of life can change surface temperature and climates. The size of life depends on the size of the green matter. When the environmental conditions are favorable, an increase in the size of photosynthesis is an inherent nature of the green matter. The surface of the earth cools down, and a cooling cycle is initiated. These cooling periods are characterized of having severe cold and dry climates. Colder surface temperature, reduced carbon dioxide content in the atmosphere, glaciers cover of land, and decreased water availability; all are unfavorable to life. The cooling cycles cannot continue indefinitely, there comes a time when the temperature in the biosphere is too cold for living matter. A large segment of life perishes as the cooling cycle progresses, which provides sediments for building continents and lands. Photosynthesis contracts in the process and the decay, oxidization, and combustion of living matter warms the biosphere and a warming or interglacial cycle is initiated. Environmental conditions become favorable for life to expand again. Only the species that adapt during the cooling cycle continue the journey of life. The warming and cooling cycles repeat throughout the geological history of the earth.

A warming cycle is much shorter than a cooling cycle. These cycles provide favorable conditions for life, and life tends to occupy the available spaces left from the devastation of the cooling cycle to the maximum extent and as quickly as possible. Figure 1 is a picture of Near Island, Alaska supporting this conclusion. The historical record indicates that the island was not covered with dense spruce trees in the late eighteenth century. Apparently, climate change has provided favorable conditions for the trees to occupy the available spaces to the maximum extent including hard floors and solid rocks. There is, of course, death and decay of living matter during warming cycles as well. However, there is more growth than decay. Consequently, the mass of sediments pro-
duced in cooling cycles is considerably greater than that of warming cycles. These sediments ultimately accumulate at ocean floors and are accreted to the continent margins by tectonics. In addition, ocean floor spreading increases during warming cycles and decreases during cooling cycles \cite{8,9}. During cooling cycles, tectonics thus builds mountains and during warming cycles tectonics build valleys, and these mountain ranges are observed around the world. Figure 2 is a satellite picture of the Andes near Bolivia. The early mountains, farthest inland, are visible, apparently due to the building of new mountains westwards. These in turn may have arrested the destructive power of winds and water from the sea and preserved some of the mountains farther inland. Mountain ranges in other parts of the world reveal these cycles as well. Generally, they have been severely eroded by rain, glaciers, and rivers. The number and duration of the cycles may be roughly estimated using map scale and extrapolating to the subduction zone. Those that appear to be preserved mountain ranges may be used to calculate the number of complete interglacial and glacial cycles and age of the mountains. Using the image of Figure 2, the average length of a complete cycle is about 4.9 kilometers. At ocean floor spreading of nearly 8.0 centimeters annually \cite{10}, the average cycle duration is nearly 122 500 years. The number of cycles may be estimated by dividing the total distance to the subduction zone, about 1 000 kilometers, by cycle length, which yields to nearly 204 cycles. This is approximately the number of cycles needed to add all of the sedimentary or soft rocks to the platform of South America. The age of the rocks may be estimated as well by knowing the actual lineal length of the material accreted to the margins of this continent. The lineal length is hard to estimate with accuracy given that much of the mountains has eroded over the years and formed the surrounding landscapes. Assuming the angle of repose of the lithified sediments as 45 degrees, the original lineal length may be estimated at 2 830 kilometers. The Andes therefore began to form approximately 71 million years ago based on these simple observations. References \cite{11,12} estimate is between 40 and 60 million years ago.

The ongoing climate change supports the derived Equation (1–r). Present deforestation and fossil fuel burning has decreased the chemical energy of the biosphere. Simultaneously, the surface of the earth has accumulated heat. Clearly, the effects of the discussed properties of the living matter are embedded in the fabrics and tissues of the biosphere. These basic properties of life apply for small samples of single cell culture to complex organisms and animals and plants. The most relevant aspect of these properties is heat exchange in the biosphere, which interacts with the laws of thermodynamics. As a result, life has changed climates and surface geology.

5. Figures

![Figure 1](https://example.com/figure1.jpg)

**Figure 1.** Picture taken by the Author of Near Island off the east coast of Kodiak Island, Alaska, U.S.A. at 57.7900° N and 152.4072° W

*Note:* Spruce trees occupy the available spaces to the maximum extent.

![Figure 2](https://example.com/figure2.jpg)

**Figure 2.** Satellite image of the Andes near Bolivia, about -20° Latitude and -65° Longitude

*Note:* The mountain chains farther inland recorded the process with which sedimentary rocks were added or accreted by tectonics. Cooling cycles provided sedimentary rocks to build mountains, and the succeeding warming or interglacial periods left valleys behind. In the direction to the ocean, cycle fingerprints have been destroyed by the elements. The picture is a courtesy of U.S. Geological Survey.

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Analysis and Discussion on Subway Construction Accidents from Geological Perspective

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ABSTRACT

Several cave-in accidents often occur in subway construction, causing personnel and economic losses. This paper has carried on the statistics and analysis of some typical subway construction accidents in recent years. Taking the collapse accident of a subway station in Hangzhou as the engineering background, the causes of the collapse of the foundation pit were analyzed. The analysis found that groundwater, earthwork over-excavation, weak support design and inadequate monitoring are the main reasons. These factors should be highlighted in the construction of similar projects in the future to avoid similar tragedies.

1. Introduction

In recent years, China’s urban rail transit construction has surged \cite{1,2}. By June 2019, 39 urban metro lines have been opened (sorted by the opening time of the first rail transit). With the development of metro lines in full swing all over the country, the metro construction accidents have arrived in quick succession, frequently ringing the alarm of safety \cite{3,4}. In the process of subway construction, the risk increases due to the properties of geotechnical complexity, unpredictable objects, the complicated construction procedures and equipment, concealment, and the permanence of construction period. Moreover, subway construction is a huge project, which needs a large number of workers. From its beginning, various risk factors have always existed. Once an accident occurs, it will cause serious casualties and property losses.

This paper gathers the typical accidents in China’s subway construction in recent years, carries out corresponding analysis, especially from the perspective of hydrogeology and soil mechanics, and puts forward some thoughts and suggestions, hoping to provide some useful advice for the follow-up engineering design and construction.

2. Accident Statistics and Description

The author collects the subway construction accidents in China in recent years.

Accident 1: On September 21, 2004, the first phase construction of Shanghai Metro Line 9 was once in dan-
A sewer was broken. The construction site was soaked in water, which caused the collapse of the ground of 700 square meters.

Accident 2: On the morning of March 28, 2007, a landslide occurred in Metro Line 10 near Suzhou Street in Beijing, and six builders were buried.

Accident 3: At 4 pm., December 17, 2007, the construction surface of Nanjing Metro Line 2 suddenly broke, which resulted in the collapse of the main road, covering an area of more than 300,000 square meters. Two trees over 10 meters high fell into the landslide. Fortunately, no casualties were caused.

Accident 4: On the afternoon of January 17, 2008, Guangzhou Metro Line 5 suddenly gushed water during construction and collapsed, resulting in a sudden subsidence of the ground near Shuangqiao Rd. under the approach span of the Pearl River Bridge. There was a large cave with an area of about 100 square meters and a depth of about 5 meters. No casualties were caused by the accident.

Accident 5: On April 1, 2008, when the construction team of Metro Line 3 in Longgang district of Shenzhen was casting concrete in place for pier, the mother slab suddenly collapsed with concrete pouring down. Five people were buried, resulting in three deaths and two injuries.

Accident 6: On November 15, 2008, a large-scale collapse occurred at the construction site of Hangzhou Metro Line 1, which caused the 75-meter pavement of Fengqing Avenue to collapse with a subsidence of 15 meters. 11 driving cars fell into the pit. The collapse of the soil outside caused the wall of foundation pit to be unstable. Then the supporting system collapsed, and a large amount of mud water flooded into the foundation pit. Four crumbling dilapidated buildings were forced to be demolished around the construction site. The residents within 500m were evacuated and transferred. 35 subway stations under construction in the city had to be suspended. This accident resulted in 21 deaths and 24 injuries, which is one of the most serious accidents in the history of metro construction in China. In this paper, the author will focus on the accident as the engineering background to analyze the cause of the accident and the measures taken, as shown in Figure 1.

Accident 7: On January 28, 2013, six collapses occurred successively near the construction site of Kangwang bus station, Liwan district of Guangzhou. Six shops collapsed and the cave-in area was about 690 square meters.

Accident 8: At 11 am, August 28, 2019, a road surface collapse occurred at the intersection of Jiangguo North Road and Stadium Road in Hangzhou (Figure 2).
3. Analysis and Discussion on the Causes of Accidents

3.1 Groundwater

In the construction process, the water in the soil has always been a nagging problem. Most of the accidents in geotechnical engineering are related to the water in the soil. In the construction process of subway stations, water is an important factor inducing accidents. According to the previous statistics, the construction accidents caused by improper water treatment account for about 21.4%.

Through the analysis of the accidents above, it is found that there are often water pipes or ground seepage around the foundation pit. For example, at the beginning of Accident 1, a small seepage appeared in the subway foundation pit, followed by a large-scale piping, and water with yellow sediment flooded into the subway foundation pit of Shanghai Metro Line 9. Meanwhile, the ground near the foundation pit began to fall, and the road about 50 meters long also collapsed in a large scale. This reason also applies in Accident 4 and Accident 6. According to the survey, the foundation soil near the Qiantang River is silty clay, and the groundwater level is high. In addition, the site is located in the main road, where traffic flow is relatively large. There are many large buses and trucks running on this road, which has brought impact on the western load-bearing wall of the foundation pit. In October 2007, a rare continuous rainfall occurred, which further increased the fluidity of soil under the foundation. Accident 8 was caused by water seepage in the construction of connecting passage of Hangzhou Metro Line 5, which resulted in pavement collapse and gas leakage.

In terms of geology and soil mechanics, due to the seepage of surface water and groundwater, the water content in the soil increases, that is, the self-weight of the soil increases, and the effective stress decreases. The seepage of water also causes a certain dynamic water pressure on the slope soil of foundation pit. Meanwhile, the accumulated water in the vertical cracks of the soil generates a certain hydrostatic pressure. On the other hand, the increase of water content in the soil causes lubrication among soil particles, and the internal friction angle of the original soil decreases greatly. As a result, the sliding force of foundation pit slope increases and the shear strength decreases, which eventually leads to the collapse of the slope and the subsidence and cave-in of the adjacent ground. Therefore, before the subway construction, it is necessary to focus on water factors which may cause accidents.

3.2 Design Factors

In Accident 6, the geology of the site is complicated, and it’s rich in groundwater. Most of the soil layers are soft clay. The engineering work such as subway foundation pit excavation and shield tunneling is like drilling a hole in the cake, which is quite risky. The specificity of the soil mechanics parameters of groundwater and soft clay should be fully considered in the design. For the stability analysis of foundation pit, it is inappropriate to use consolidated undrained strength index and saturated unit weight for saturated clay. The design team has not paid enough attention to the particularity of soft clay.

When it comes to piles, walls and inner strut in deep soft soil areas, stability in depth must be considered, including pile and wall settlement, upheave and “skirting” damage, which should be strictly calculated by various methods. If it cannot meet the requirements, it should deepen the depth of pile and wall into soil or reinforce the passive area. In Accident 6, the project design has not paid enough attention to this, and no passive zone reinforcement has been carried out.

3.3 Construction Factors

The quality of a project ultimately depends on the quality control of construction. One of the most important reasons in accident 6 is that the steel support booster was not added enough, which made the bearing capacity of the protective wall insufficient. Generally speaking, the booster should be added to more than 200 tons, even 300 tons in geological conditions such as Hangzhou, but in terms of the accident site, it is certainly not enough.

In addition, the protective wall of the west subway section underwent tremendous deformation. The sliding of the protective wall had occurred sometime before the accident. Earlier, many on-site construction workers had also noticed cracks on the wall, but no measures were taken. Besides, serious road subsidence and multiple cracks occurred one month ago, which actually reflected the change of soil mass, but it was still ignored as a result of excessive traffic flow by the construction team. Moreover, in the construction process, the foundation pit was seriously over-excavated. The supporting system had serious defects. The steel pipe support was not timely erected, and the cushion was not timely poured, either.

Because of the short construction period, many details were neglected in order to rush to meet the deadlines, which actually caused management omissions. For example, in the subway station, if the open excavation starts, the multi-section construction method must be strictly implemented, and every 20 meters should be segmented.
However, after the accident, it was found that the interval between sections was 60 meters. Although it is difficult to establish a direct causal relationship between the shortening of construction period and cave-in accidents, facts show that the shortening of construction period indirectly promotes the occurrence of accidents to a certain extent, so that dangers which could have been discovered are ignored intentionally or unintentionally.

3.4 Monitoring Measurement

There must be an omen before the foundation pit collapses. The monitoring data of the foundation pit will certainly give an alarm according to the daily reports. General monitoring items include horizontal displacement and settlement monitoring, inclinometer monitoring, stress monitoring, earth pressure monitoring, water level monitoring.

In Accident 6, the soil near the station was relatively soft with high fluidity. The pressure caused by the traffic flow on the west Fengqing Avenue led to the soil layer below moving toward the subway construction site. In addition, the previous rainfall caused the surge of river in the east. The softer soil also increased the mobility of the soil layer. Under this background, monitoring data such as horizontal displacement, earth pressure and water level change should be able to detect the abnormal situation in advance and send out an alarm so that the construction team could take corresponding measures. But in that situation, this was obviously not well tackled.

4. Some Reflections

(1) Make a good pre-construction survey. With the deepening excavation of foundation pit, the risk of confined water is also increasing, which can easily break through the weak stratum, resulting in piping and drift sand. Therefore, a good survey should be made before the construction of foundation pit. The features of the site, the adjacent aquifers, and the hydraulic relations between aquifers and surface water should be clarified. Then make a design of dewatering.

(2) In the engineering design, it’s inappropriate to use consolidated undrained strength index and saturated unit weight to calculate the strength of groundwater subsoil, to analyze the stability and to check the bottom upheave. The highly sensitive soft soil was not given enough attention and no effective measures were taken. A mistake was made at the time when Fengqing Avenue was not closed. The checking calculation of pit overload based on consolidated undrained strength was also dangerous. In addition, according to the disturbance degree of the subsoil, the disturbed soil is strengthened by layers.

(3) In the construction process, it is necessary to ensure the construction quality of the underground continuous wall, and dewatering should be carried out according to the design.

(4) Strengthen monitoring and measurement. During the excavation of the foundation pit, it is necessary to ensure the safety of the pit, the surrounding buildings and underground pipelines. Therefore, in the construction process, informationized monitoring of foundation pit and its surroundings should be strengthened, and the monitoring data should be promptly sent to the construction team.

(5) Eliminate man-made accidents from institutional mechanisms. Eliminate illegal subcontracting, and set the construction period from a scientific development perspective, which cannot be guided by the leadership’s thinking. Many metro projects are constructed underground, which is highly risky. Therefore, a more complete technical support system and a stricter monitoring and risk management should be required.

References


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